



# 3<sup>rd</sup> **ASTERICS-OBELICS Workshop**

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# Recent developments in LOFAR calibration & imaging

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# Reminder: imaging

- The *visibility*  $y$  for antennas  $i, j$ , channel  $q$ , time  $t$  given by:

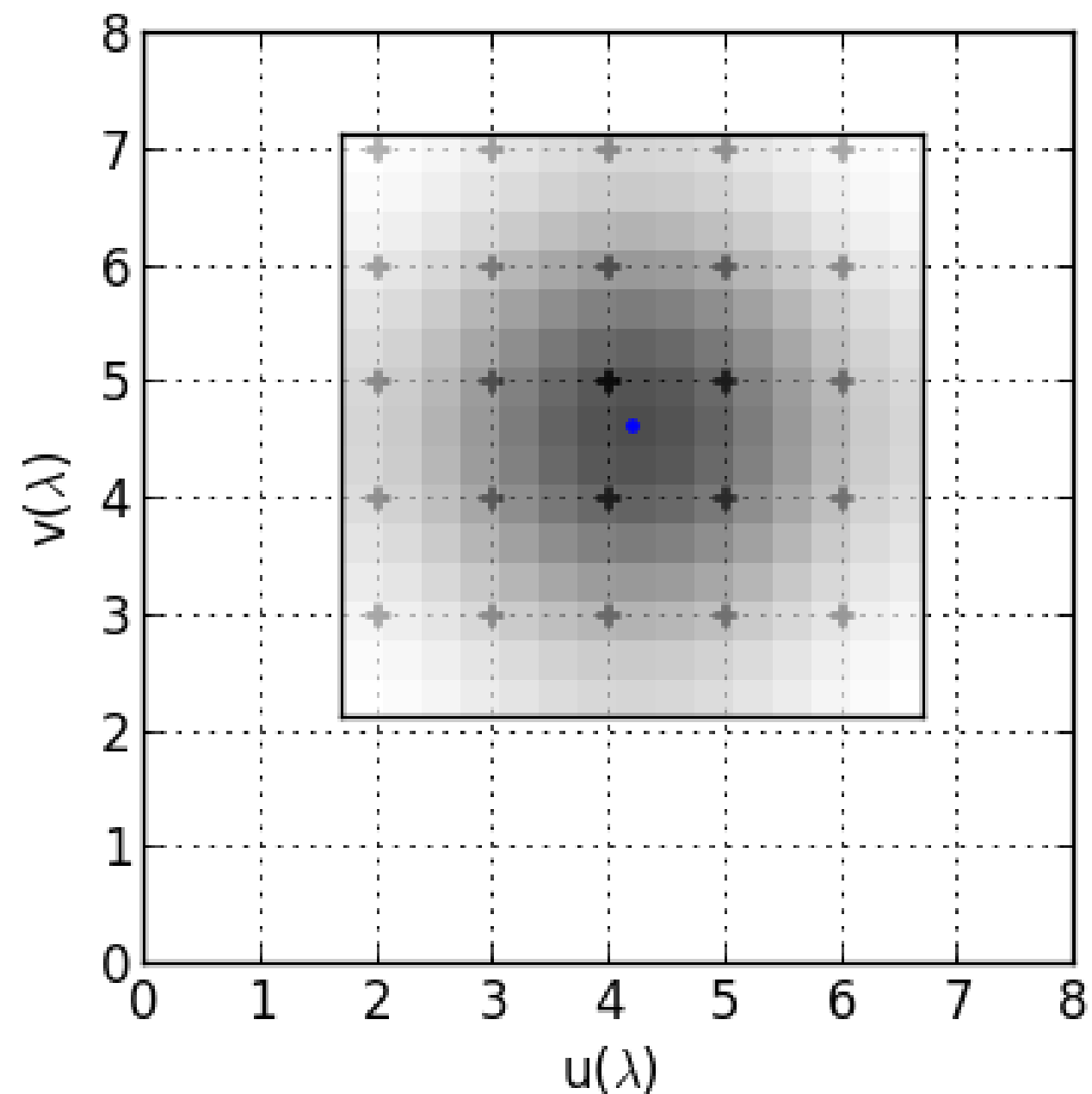
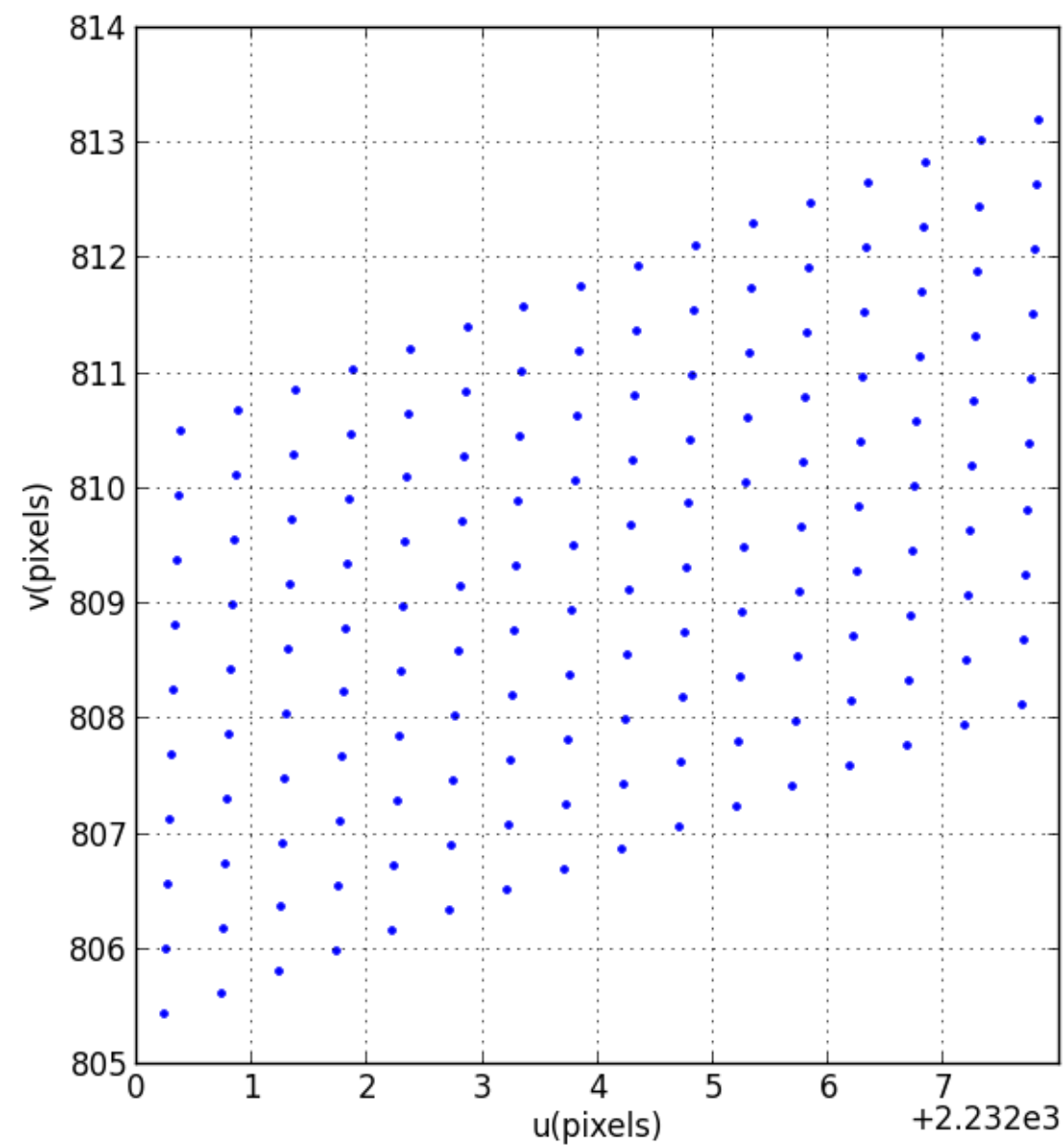
$$y_{ijqr} = \iint_{lm} e^{-j2\pi(u_{ijr}l + v_{ijr}m + w_{ijr}n)/\lambda_q} g_{iqr}(l, m) g_{jqr}^*(l, m) I(l, m) dl dm$$

- $I(l, m)$  is the image we're interested in.
- Direct inversion impossible:
  - number of  $l, m$  pixels  $\sim 10^9$ , number of visibilities  $\sim 10^9$
- Use FFT!



# Convolutional resampling

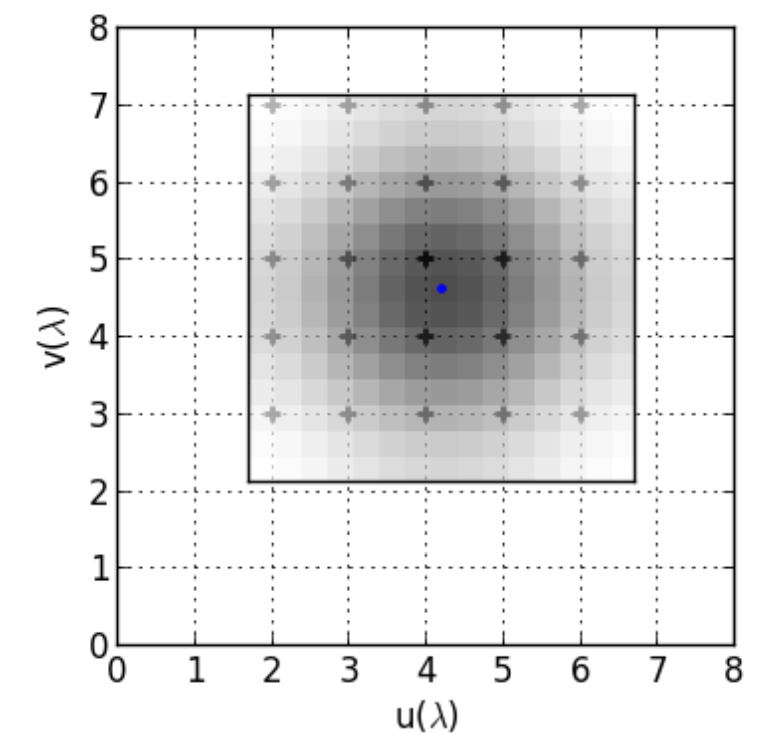
- FFT needs data on regular grid



# Instrumental effects

- Convolution applies a multiplication in the image domain. The same convolution can be used for applying instrumental or atmospheric effects.
- Can become very expensive for fast varying effects.

$$y_{ijqr} = \iint_{lm} e^{-j2\pi(u_{ijr}l + v_{ijr}m + w_{ijr}n)/\lambda_q} g_{iqr}(l, m) g_{jqr}^*(l, m) I(l, m) dl dm$$



# Image domain gridding (IDG)

- Image domain gridding applies kernel in image domain. Needs going back and forth to image domain, costs a lot more computation.
- Operations in IDG are much more effective in memory, fit very well on GPUs.

# Image domain gridding: status

- Optimized implementations for many platforms (by Sebastiaan van der Tol & Bram Veenboer)
  - CPU: Intel Haswell, Xeon Phi
  - GPU: Nvidia & AMD
  - FPGA (ongoing)
- Integrated in wsclean (established imager), code available at <https://gitlab.com/astron-idg/idg>
- Algorithm published: [A&A 616, A27 \(2018\)](#)
- Implementation papers forthcoming.
- Shown working on LOFAR, MWA & ASKAP data.

# Calibration

- The *visibility*  $y$  for antennas  $i, j$ , channel  $q$ , time  $t$  given

$$y_{ijqr} = \iint_{lm} e^{-j2\pi(u_{ijr}l + v_{ijr}m + w_{ijr}n)/\lambda_q} g_{iqr}(l, m) g_{jqr}^*(l, m) I(l, m) dl dm$$

- Direction independent calibration:  $g_{iqr}(l, m) = g_{iqr}$
- Can be found from model visibilities.
- Risk: overfitting.



# Direction-independent calibration

- Find  $\hat{G} = \operatorname{argmin}_G \|V - GMG^H\|_{\text{frob}}^2$ .
- $V$  is a matrix of observed visibilities.  
 $V_{pq}$  is correlation between signal from station  $p$  and  $q$ .
- $M$  is a matrix of model visibilities.
- $G = \operatorname{diag}(g)$  is unknown matrix of gains,  $g_p = e^{i\phi_p}$
- $G$  contains corrections for effects such as wrong cable lengths, drifting clocks, electronic gains, and delays due to the ionosphere.
- Challenge: parametrize  $G$  with few parameters.

# Calibration: stefcal (ADI)

- Goal: find  $\hat{G} = \operatorname{argmin}_G \|V - GMG^H\|_{\text{frob}}^2$
- Idea:
  - Fix  $G$ , solve for  $G$
  - Fix  $G$ , solve for  $G$  (same computation)
  - Average:  $G^{(i)} = \frac{1}{2}(G + G)$
  - Iterate
- Given  $G$ ,  $G = \operatorname{diag}(g_p)$  simply  $g_p^{\leftarrow} = \frac{(GM)_{\kappa,p} \cdot V_{\kappa,p}}{(GM)_{\kappa,p} \cdot (GM)_{\kappa,p}^H}$

# Constrained calibration

- Iterations in `stefcal` can be interleaved with constraining operations, that restrict solutions to satisfy e.g. a given frequency dependency (physical).
- Limits number of free parameters, overfitting.
- Still converges (if constraint is linear).

# Calibration forms

Calibration: find  $\{G_p\}$  to minimize

station p

$$k G_p V_{pq} G_q^H - M_{pq} k$$

measured

model

$G_p$  can be restricted to:

# unknowns  
per station

- Full Jones

$$G_p = \begin{pmatrix} A_{xx}^{(p)} e^{i\varphi_{xx}^{(p)}} & A_{xy}^{(p)} e^{i\varphi_{xy}^{(p)}} \\ A_{yx}^{(p)} e^{i\varphi_{yx}^{(p)}} & A_{yy}^{(p)} e^{i\varphi_{yy}^{(p)}} \end{pmatrix}$$

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- Diagonal

$$G_p = \begin{pmatrix} A_{xx}^{(p)} e^{i\varphi_{xx}^{(p)}} & 0 \\ 0 & A_{yy}^{(p)} e^{i\varphi_{yy}^{(p)}} \end{pmatrix}$$

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- Phase only

$$G_p = \begin{pmatrix} e^{i\varphi_{xx}^{(p)}} & 0 \\ 0 & e^{i\varphi_{yy}^{(p)}} \end{pmatrix}$$

2

- Common phase

$$G_p = \begin{pmatrix} e^{i\varphi^{(p)}} & 0 \\ 0 & e^{i\varphi^{(p)}} \end{pmatrix}$$

1



# Calibration: status

- Stefcacal extended to include direction dependent effects (Smirnov & Tasse 2015).
- Constrained calibration part of DPPP, joint work with André Offringa  
Diepen, G., & Dijkema, T.J. 2018, Astrophysics Source Code Library, ascl:1804.003
- Code available at <https://github.com/lofar-astron/DP3>
- Used in prefactor, the default LOFAR calibration pipeline.

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