

Ionospheric Effects

LOFAR data school 2024

M. Mevius

Ionosphere: imaging

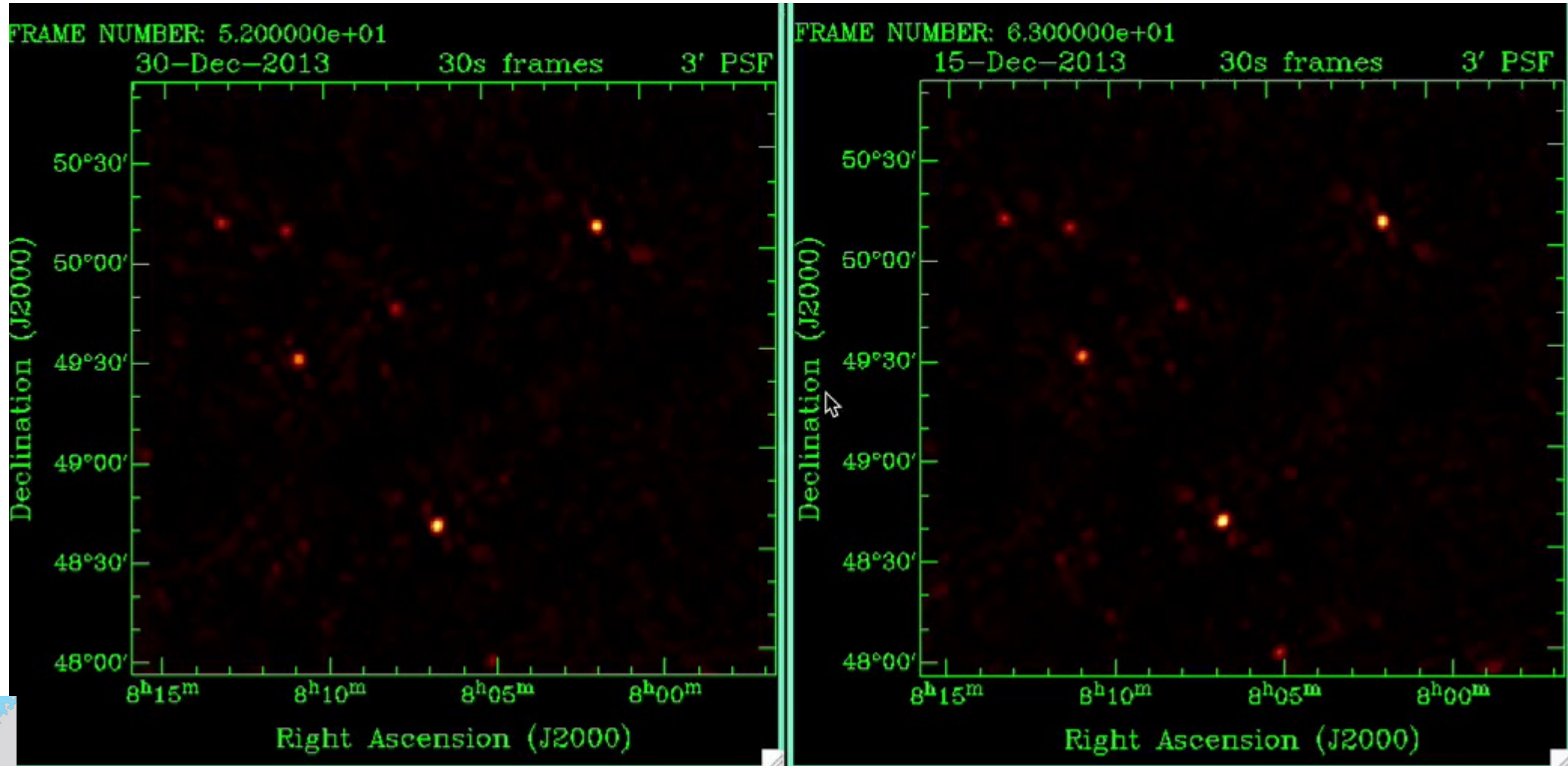
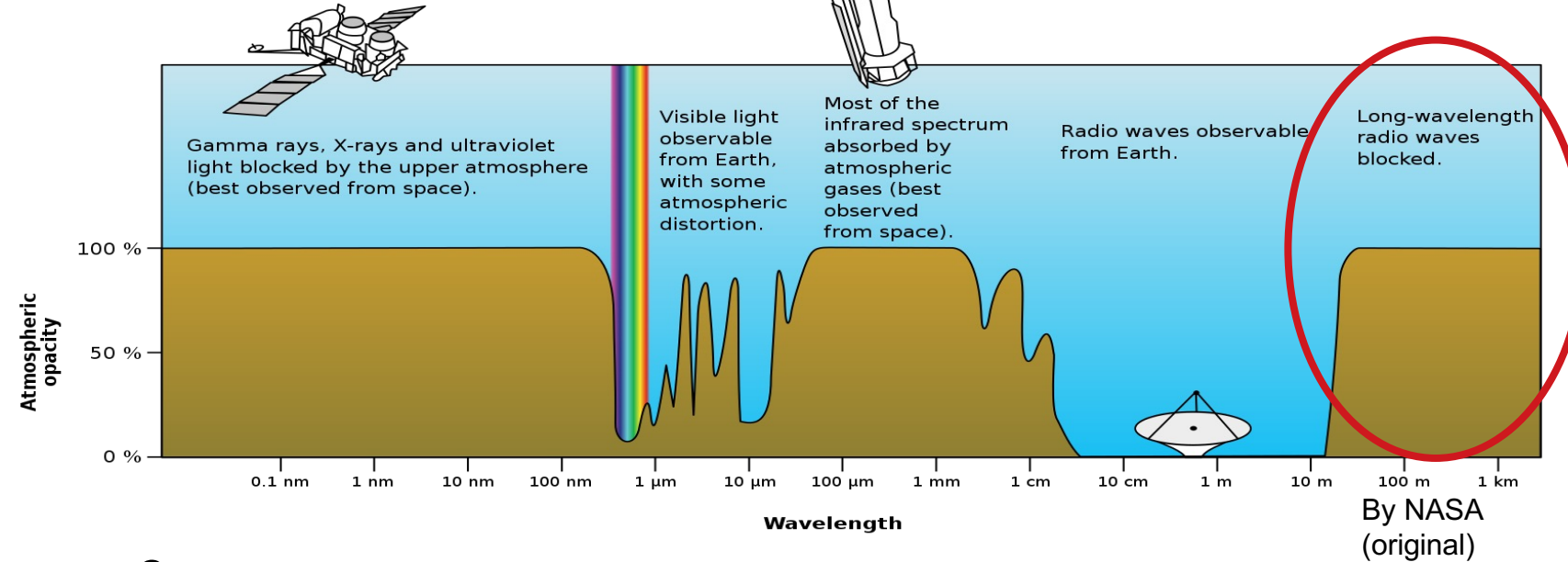


Image credit: G. de Bruyn



Ionosphere



What is it and why do we care?

1950s formally defined as: “the part of the earth’s upper atmosphere where ions and electrons are present in quantities sufficient to affect the propagation of **radio waves**”

Encyclopedia Britannica

Ionized layer(s) in the upper atmosphere,
altitudes between 50 and 1000 km
Long distance radio transmission: bouncing via ionosphere

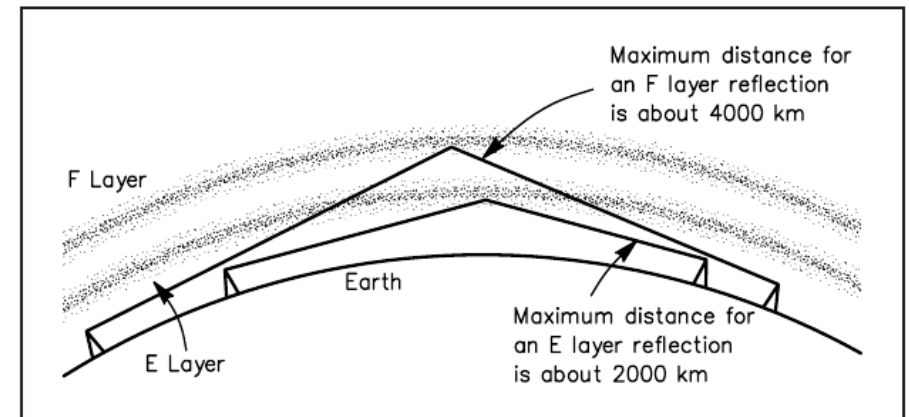
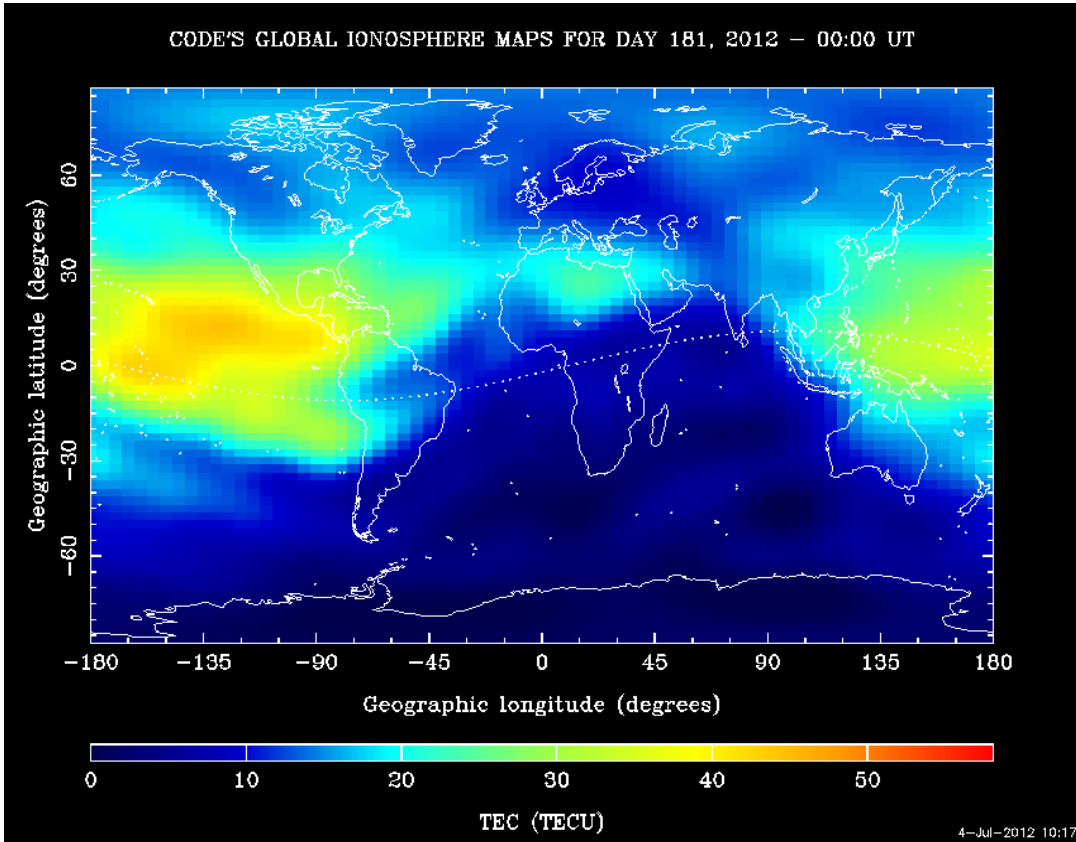


Figure 6—Signals reflected by the E and F layers. Ian Poole, G3YWX

Electron Density

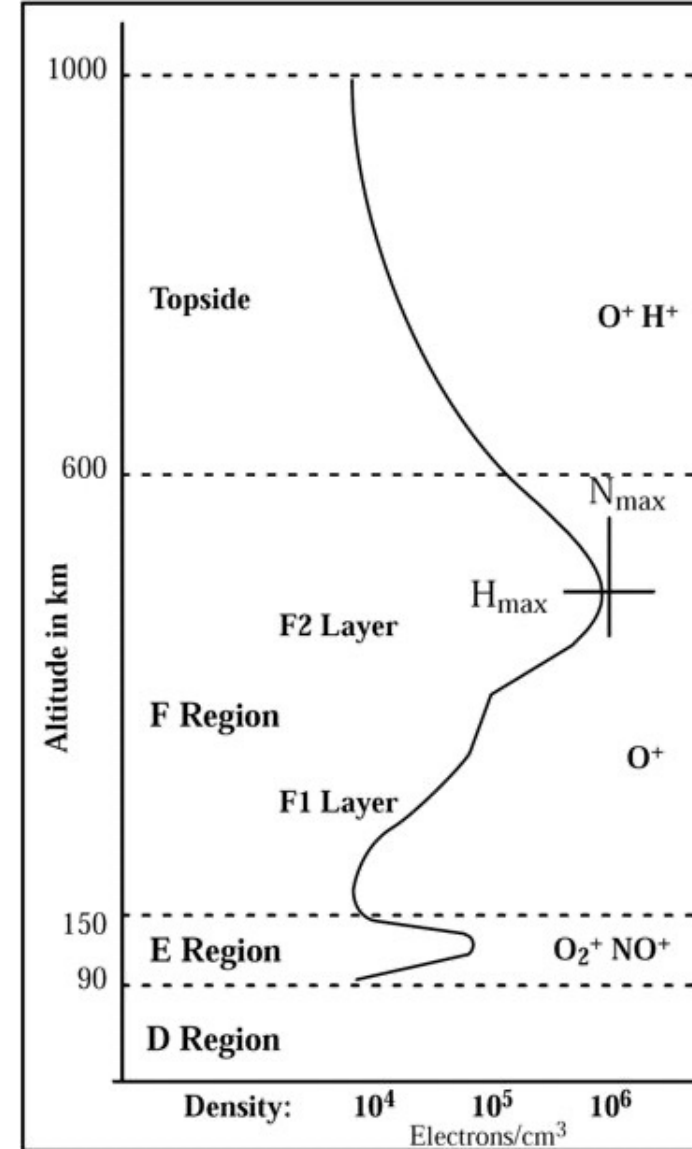
Electron density/Total integrate electron density (TECU: $10^{16} \text{ e}^-/\text{m}^2$)
Typical values @ 52° for integrated TEC along LOS: $\sim 5(\text{night}) - 30(\text{day})$ TECU



Ionization through solar radiation (X+EUV)
Recombination at night

Depth of radiation + Molecular densities + composition:
Layered structure
Maximum around 300 km (F-layer)

In many models thin screen approximation



Ionospheric Variability

The ionosphere is highly dynamic:

Ionization through solar radiation (UV+X-ray)
Recombination at night

→ diurnal pattern

large gradients @ dusk and dawn

Solar activity cycle

Space Weather events

Scintillation (high turbulence):

(often) after sunset

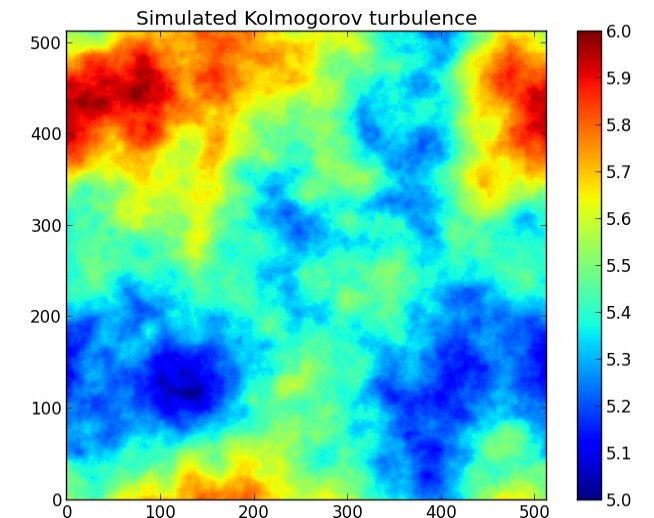
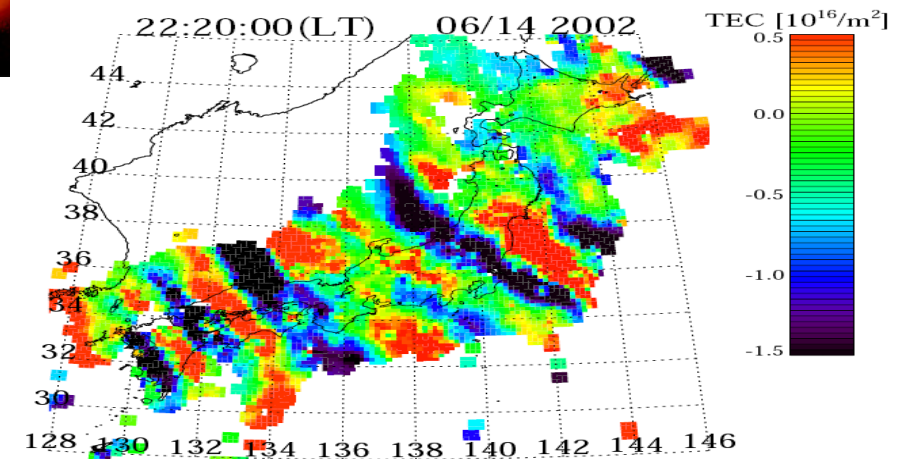
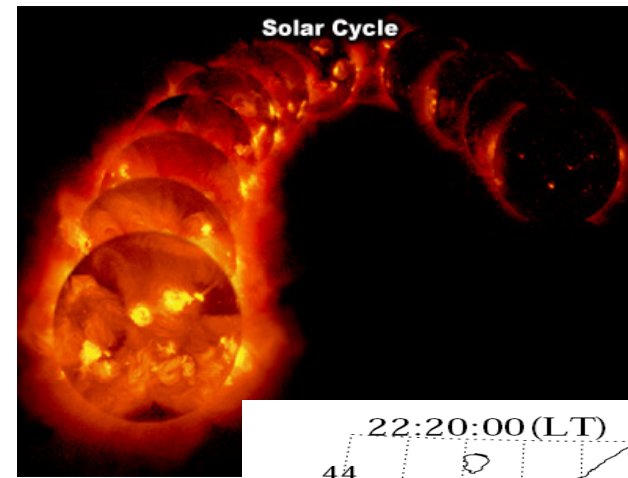
Pressure + composition lower atmosphere

Traveling Ionospheric Disturbances (TIDs)

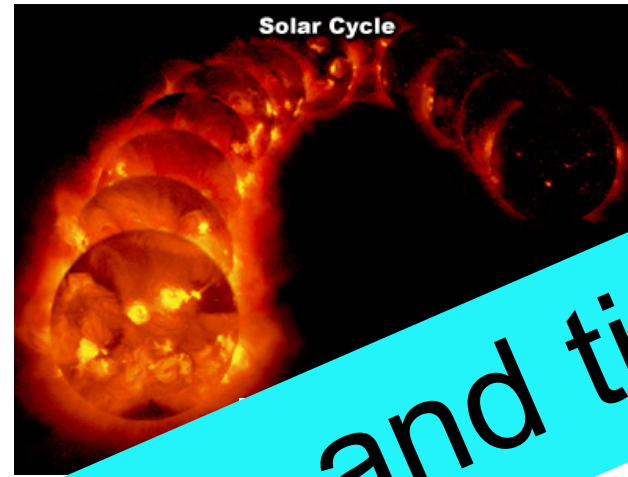
Small Scale Structures: Kolmogorov turbulence

Structures moving with speeds ~ few 100 km/hr

When observing: tracking through the ionosphere



Ionospheric Variability



The ionosphere is highly dynamic:

Ionization through solar radiation (UV+X-ray)

Recombination at night

→ diurnal pattern

large gradients @

Solar activity cycle

Space Weather

Scintillation

Pre-sunset spread-F after sunset

Pre-sunset spread-F lower atmosphere

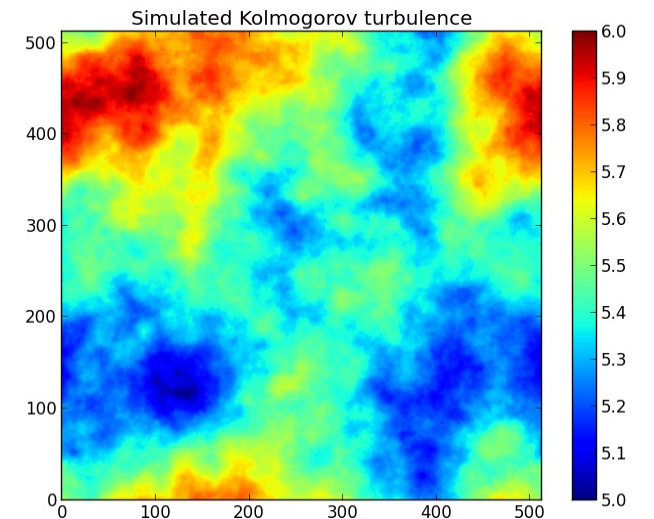
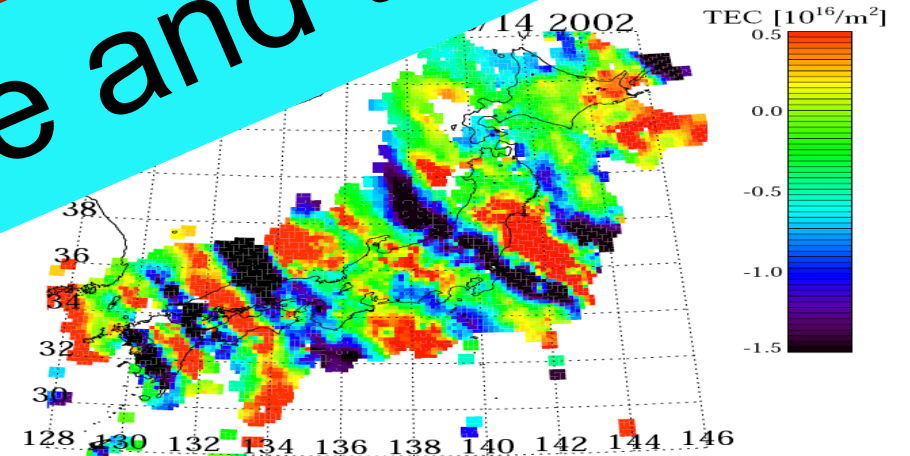
Travel Ionospheric Disturbances (TIDs)

Small Scale structures: Kolmogorov turbulence

Structures moving with speeds ~ few 100 km/hr

When observing: tracking through the ionosphere

Varies a lot in space and time!



Electromagnetic Propagation

Total integrated propagation delay

Refractive index in ionized plasma

$$\Phi_{\text{ion}} = -\frac{2\pi\nu}{c} \int_{\text{LoS}} (n - 1) dl.$$

Approximation for frequencies well above the plasma frequency

$$n \approx 1 - \frac{q^2}{8\pi^2 m_e \epsilon_0} \cdot \frac{n_e}{\nu^2} \pm \frac{q^3}{16\pi^3 m_e^2 \epsilon_0} \cdot \frac{n_e B \cos \theta}{\nu^3} - \frac{q^4}{128\pi^4 m_e^2 \epsilon_0^2} \cdot \frac{n_e^2}{\nu^4} - \frac{q^4}{64\pi^4 m_e^3 \epsilon_0} \cdot \frac{n_e B^2 (1 + \cos^2 \theta)}{\nu^4},$$

Appleton–Hartree equation (Taylor expansion)

Electromagnetic Propagation

Total integrated propagation delay

Refractive index in ionized plasma

$$\Phi_{\text{ion}} = -\frac{2\pi\nu}{c} \int_{\text{LoS}} (n - 1) dl.$$

Approximation for frequencies well above the plasma frequency

$$n \approx 1 -$$

1st order: dispersive phase delay
 $\Delta\phi = 8.45\text{e}9 \text{ dTEC}/\nu$

2nd order: Faraday Rotation

3rd order
 (LBA < 50MHz)
 $\Delta\phi \sim 1/\nu^3$

~~$$-\frac{q^4}{64\pi^4 m_e^3 \epsilon_0} \cdot \frac{n_e B^2 (1 + \cos^2 \theta)}{\nu^4},$$~~

Appleton–Hartree equation (Taylor expansion)

Electromagnetic Propagation

Calibration: Jones matrices

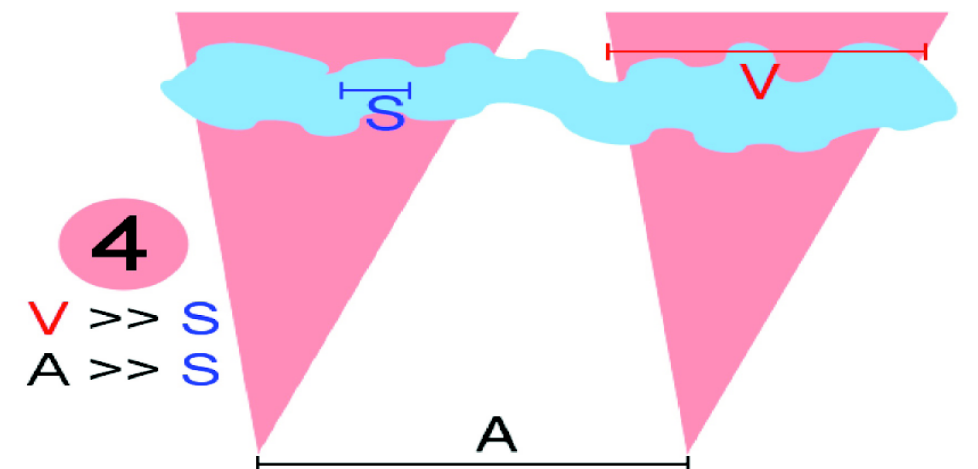
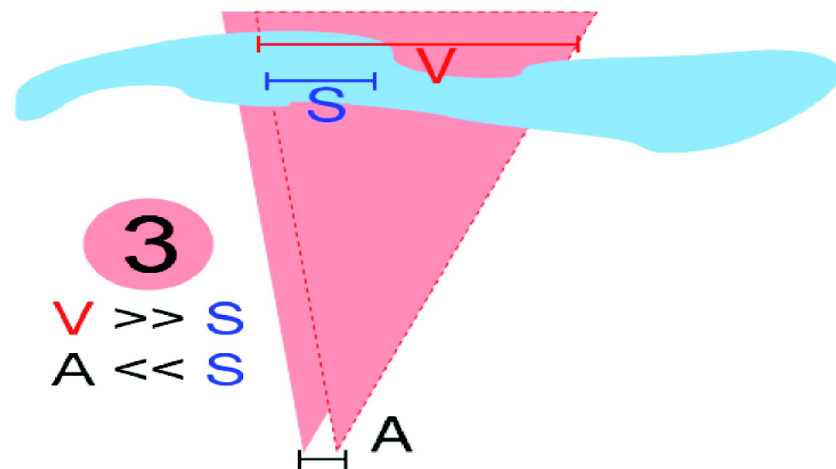
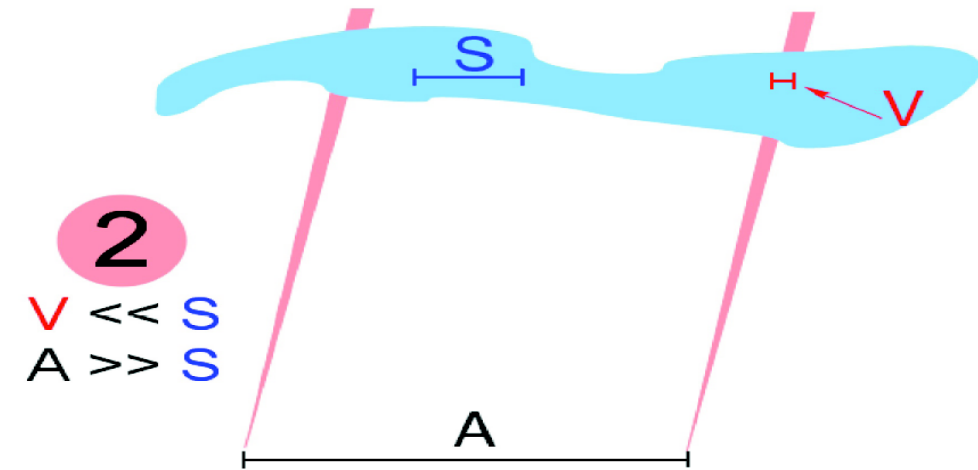
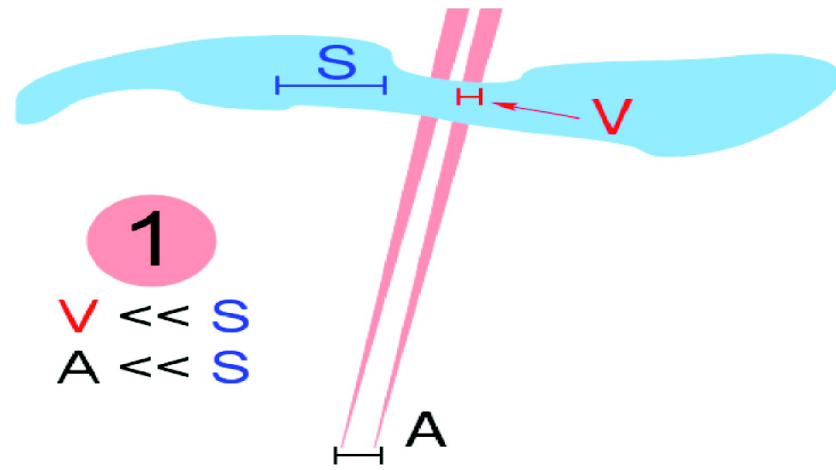
$$\begin{pmatrix} G_{xx} & G_{xy} \\ G_{yx} & G_{yy} \end{pmatrix} = \begin{pmatrix} \cos(\alpha) & \sin(\alpha) \\ -\sin(\alpha) & \cos(\alpha) \end{pmatrix} \cdot \begin{pmatrix} G_{xx} & 0 \\ 0 & G_{yy} \end{pmatrix}$$

Refractive index in ionized plasma

$$n \approx 1 - \frac{q^2}{8\pi^2 m_e \epsilon_0} \cdot \frac{n_e}{v^2} - \frac{q^3}{16\pi^3 m_e^2 \epsilon_0} \cdot \frac{n_e B \cos \theta}{v^3} - \frac{q^4}{128\pi^4 m_e^2 \epsilon_0^2} \cdot \frac{n_e^2}{v^4} - \frac{q^4}{64\pi^4 m_e^3 \epsilon_0} \cdot \frac{n_e B^2 (1 + \cos^2 \theta)}{v^4},$$

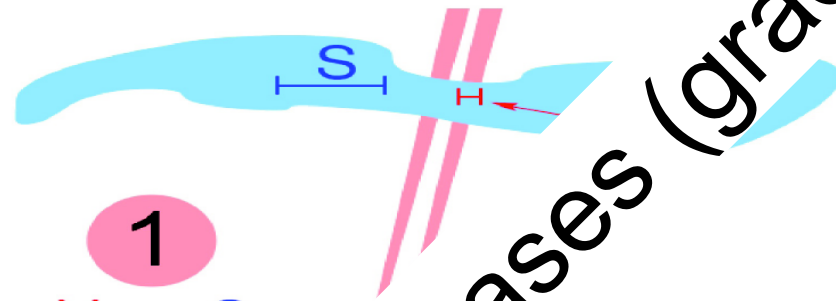
Appleton–Hartree equation (Taylor expansion)

Phase effects



Phase effects

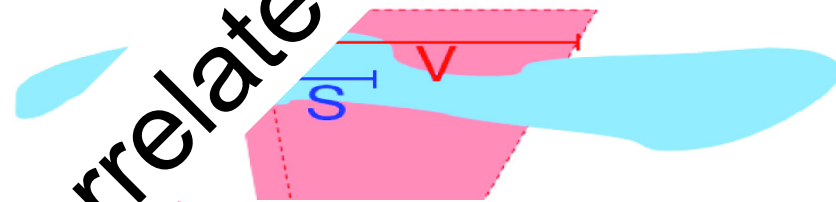
Correlated Phases (gradients)



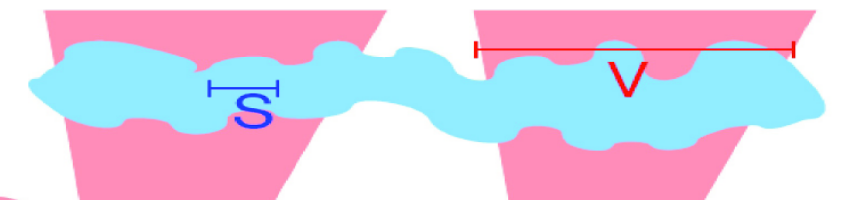
1
 $V \ll S$
 $A \ll S$



2
 $V \ll S$
 $A \gg S$

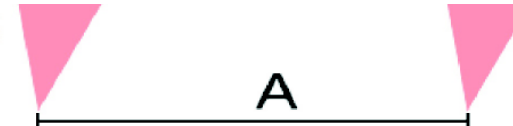


3
 $V \gg S$
 $A \ll S$

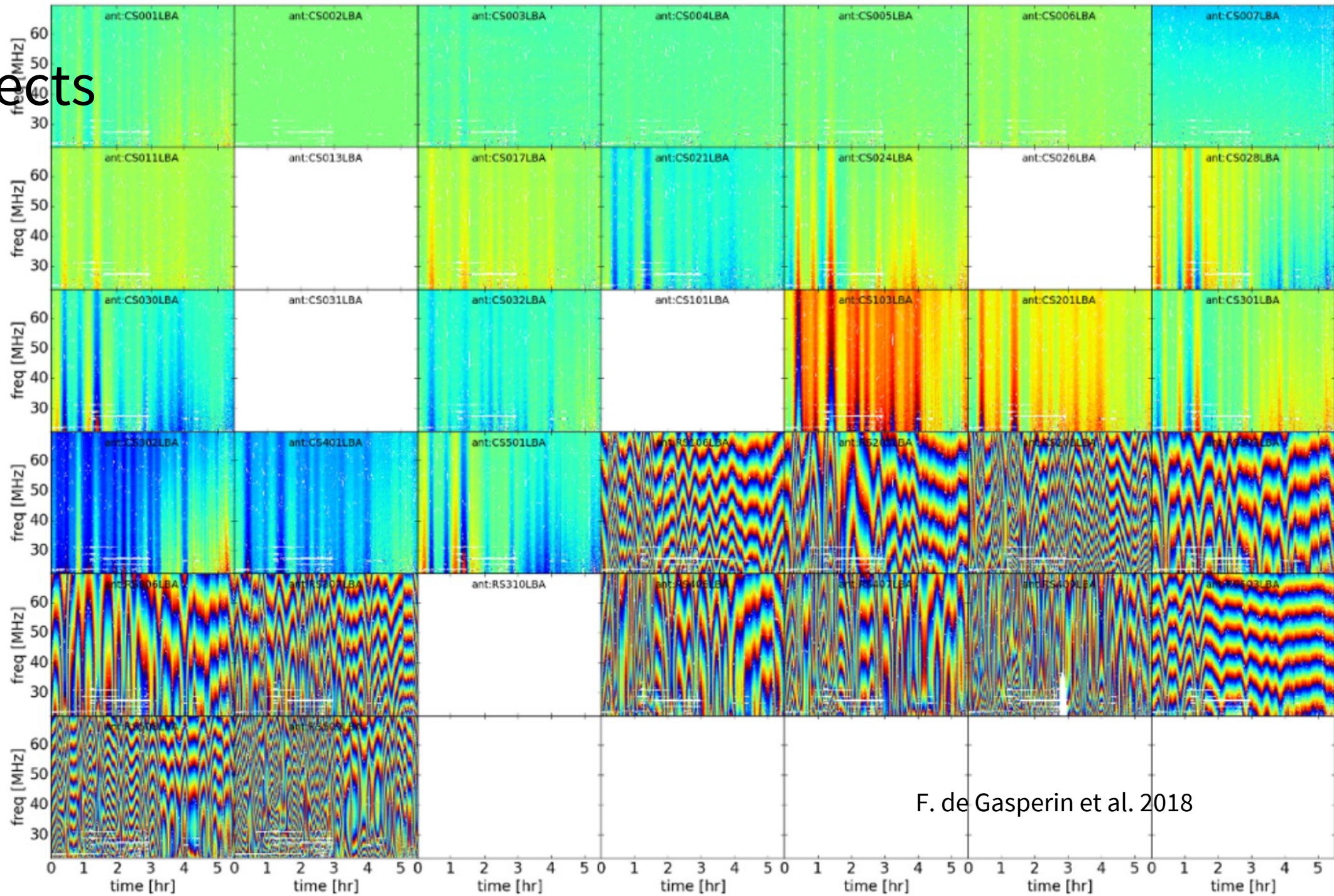


$A \gg S$

Direction Dependent Calibration



Phase effects

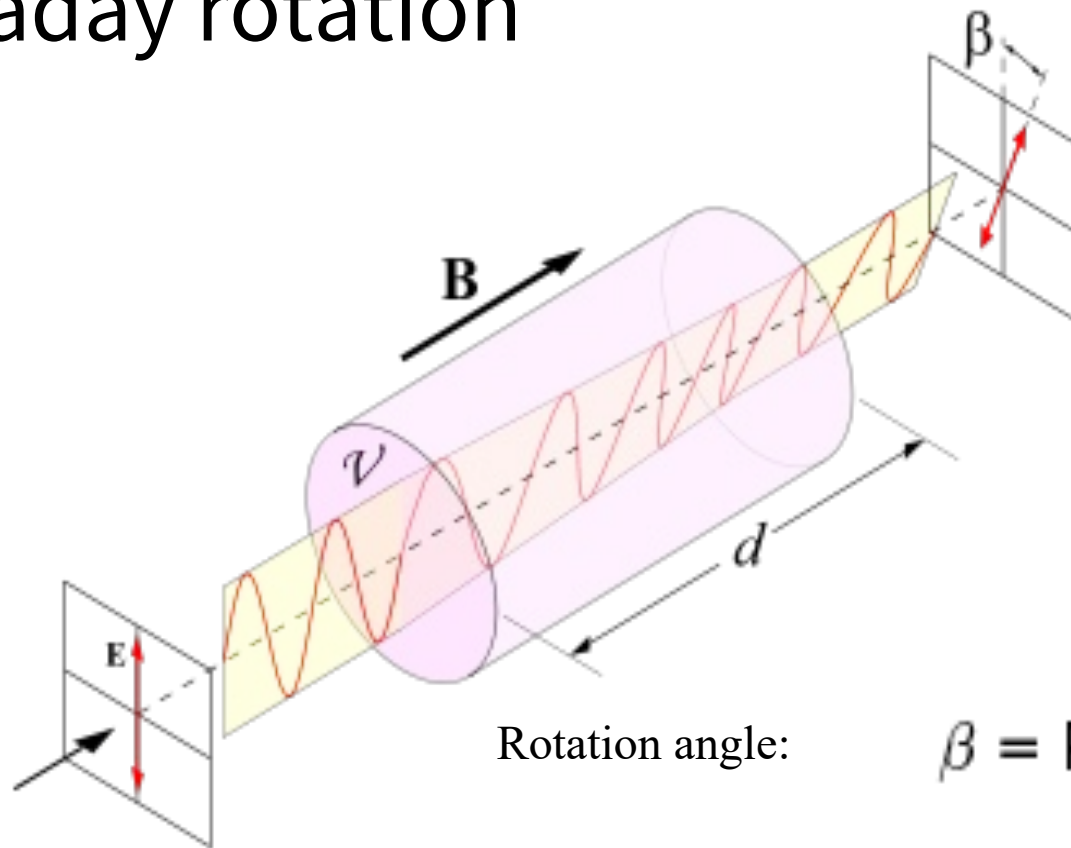


F. de Gasperin et al. 2018

See Polarimetry Lecture (M. Brentjens)
on Wednesday

Polarisation Effects

Faraday rotation



Plasma + magnetic field:
phase shift between right and left circular
components

Equivalently:

Rotation of linearly polarized components

$$\beta = RM\nu^{-2}, \quad RM = \frac{e^3}{8\pi^2\epsilon_0 m^2 c^3} \int_0^d n_e(s) B_{||}(s) ds$$

Differential Faraday Rotation

Thin layer approximation: $RM_{iono} = TEC \cdot B_{\parallel}$

Different LOS: $dTEC$ and $dB_{\parallel} \rightarrow dRM$

Rotation of the signal from XX,YY to XY,YX due to different Faraday rotation angles for different antennas

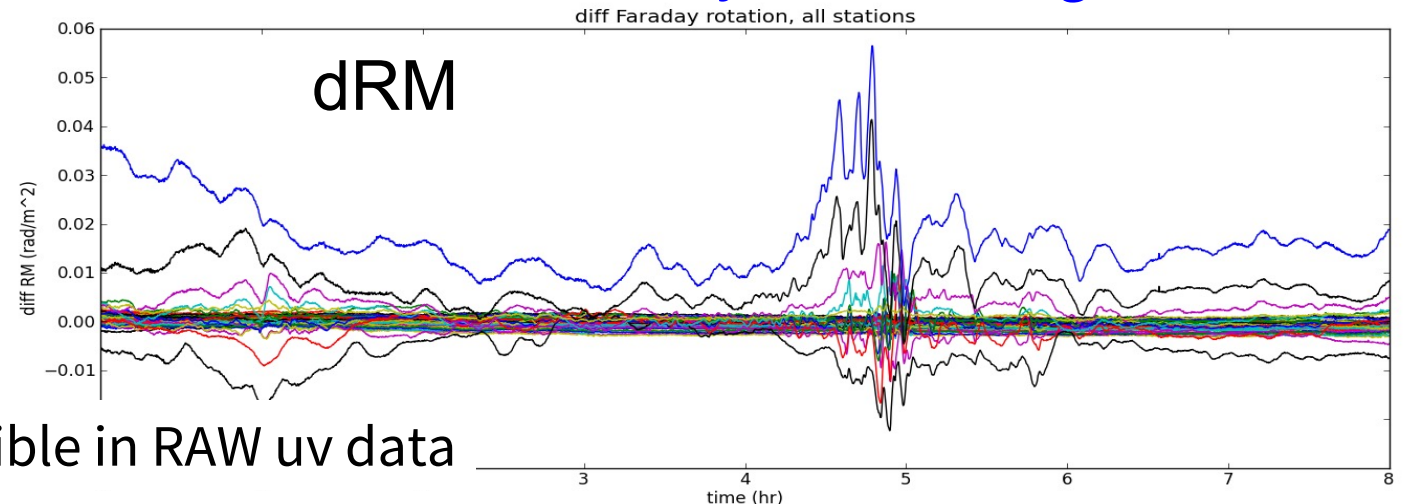
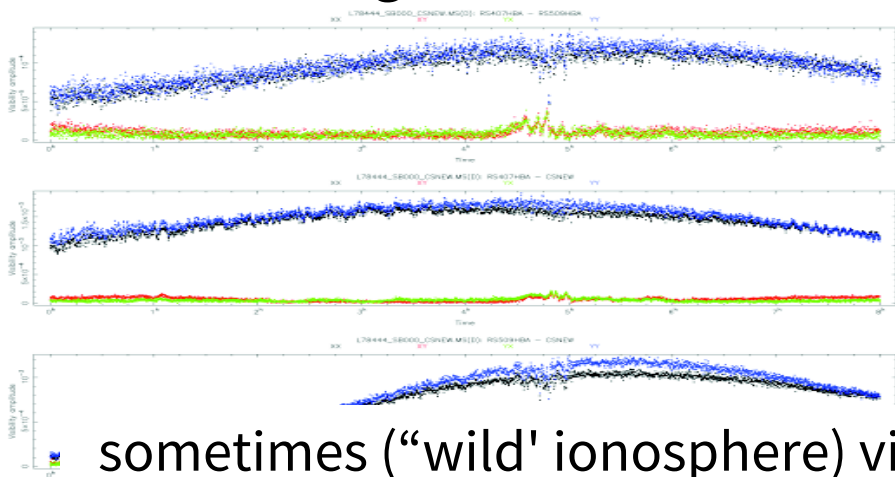
>100MHz: small rotation most of the time

<100MHz: significant effect

Selfcal: either

- solve full polarization matrix
- diagonal gains + 1 rotation matrix
- convert to circular polarization:

difference in R and L phases gives Faraday rotation angle



sometimes ("wild" ionosphere) visible in RAW uv data

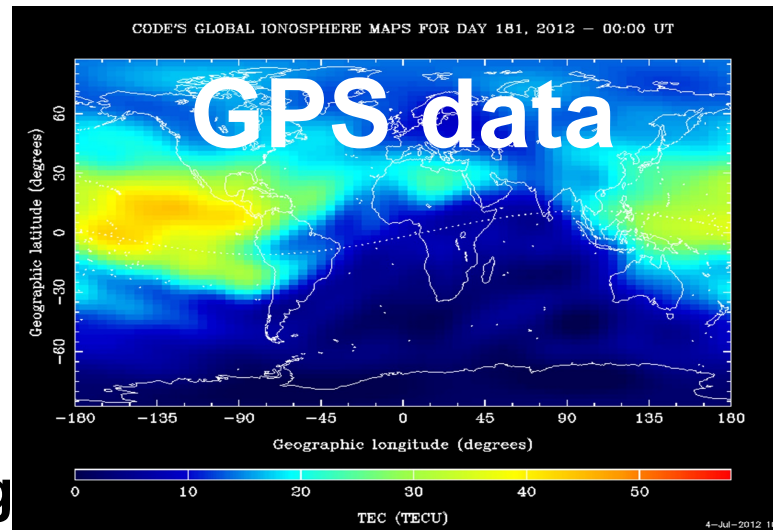
Faraday rotation: Polarised emission

Polarized emission

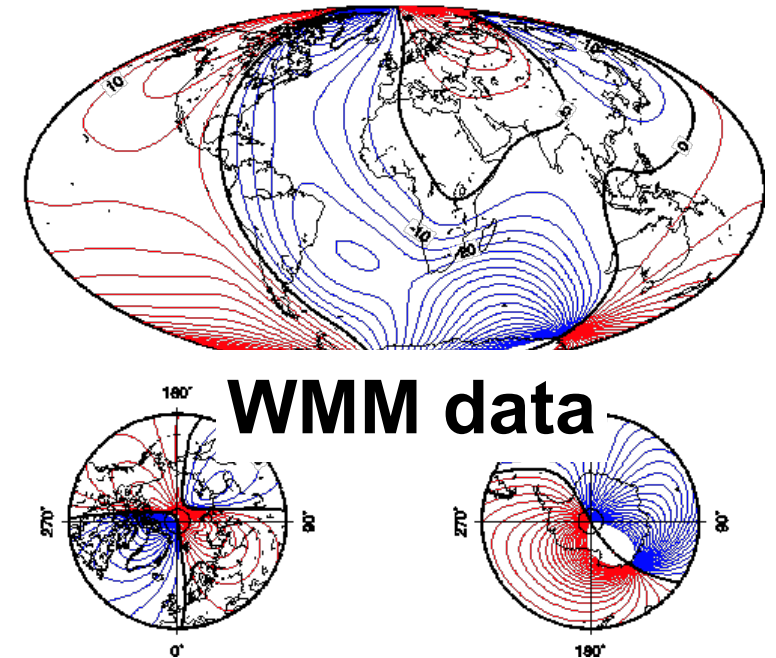
Time variability of ionospheric Faraday rotation causes depolarization

Model RM_{iono} by combining geomagnetic and ionospheric models

Eg: <https://github.com/lofar-astron/RMextract>

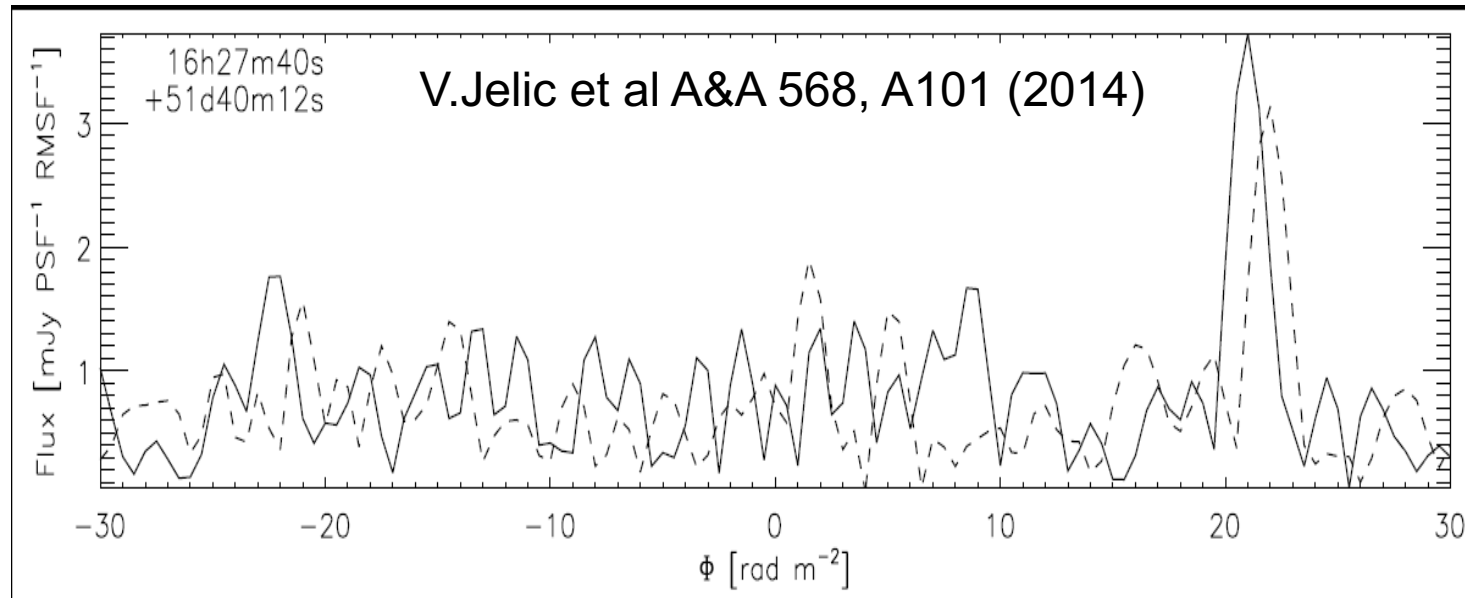


WMM2010 Declination (min)

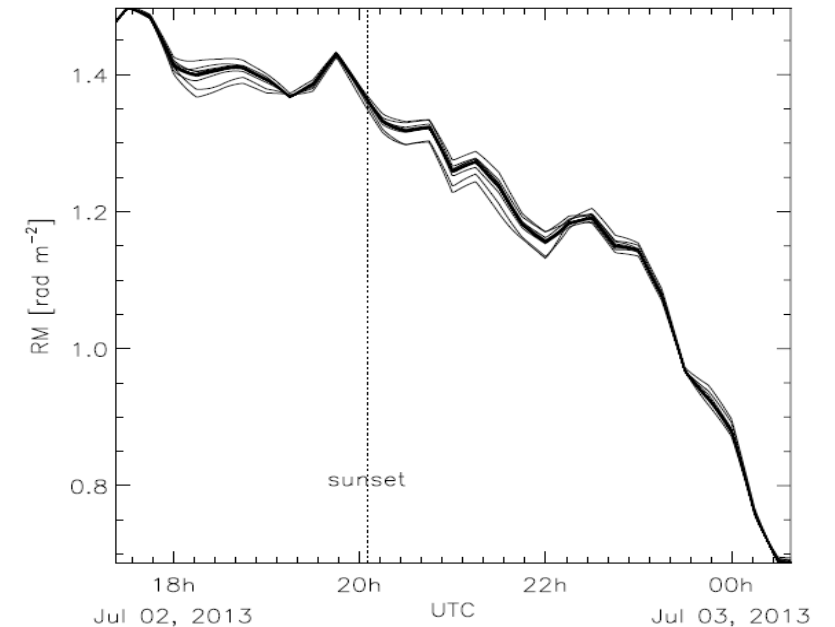


$$\text{Thin layer approximation: } RM_{iono} = \text{TEC} \cdot B_{\parallel}$$

Faraday rotation: Polarised emission



Polarized Flux before (dashed) and after (solid) RM correction

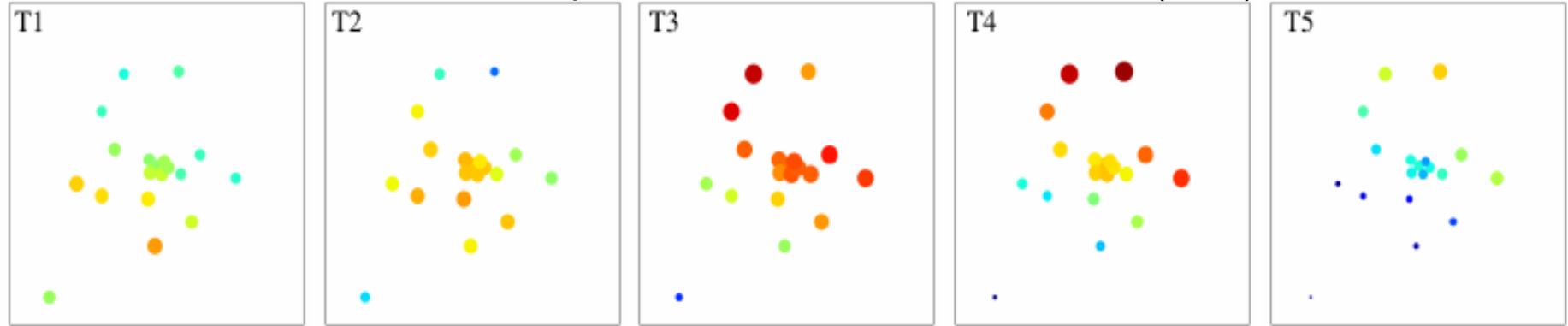


Ionospheric RM corrections versus time

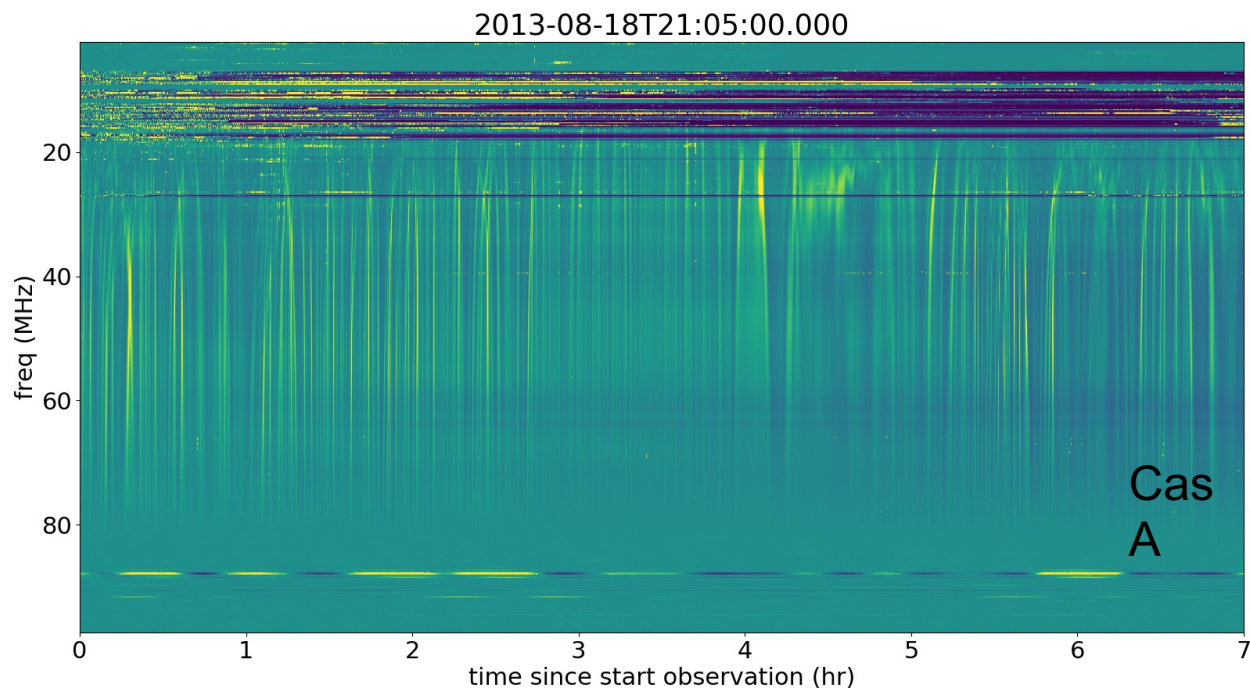
Thin layer approximation: $RM_{\text{iono}} = \text{TEC} \cdot B_{\parallel}$

Amplitude Effects

Amplitude solutions LOFAR CORE (3km)



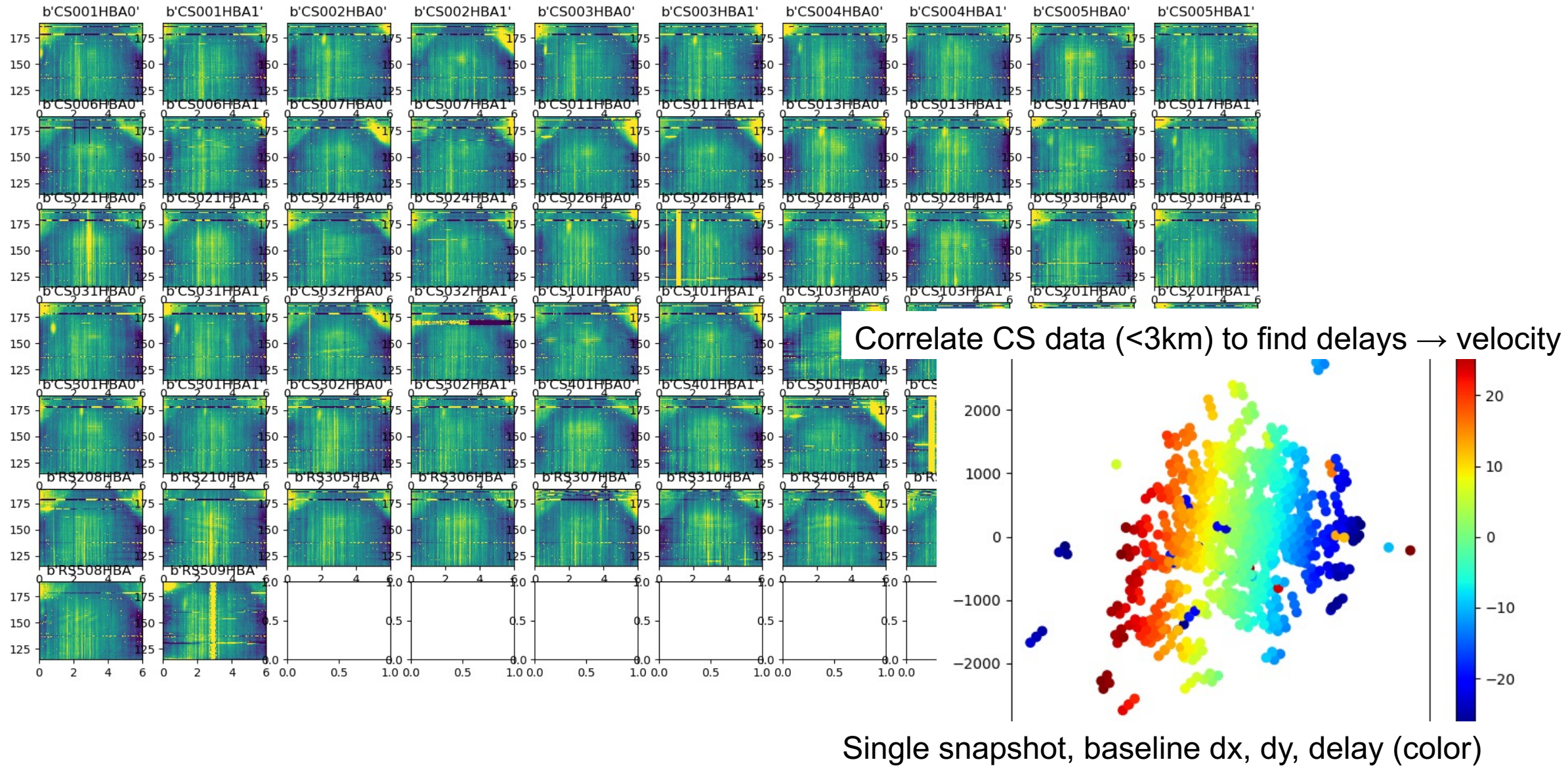
F. de Gasperin et al. 2018



Amplitude scintillation:

- Due to lensing effect (Fresnel scale: ~ 2 km @LOFAR)
- Rapid varying station amplitudes
- DI calibration
- FOV variations?
- Excellent diagnostic tool for ionospheric conditions

Characterization of the ionosphere: Autocorrelations of the calibrator (3C196, HBA)



Conclusion

- When doing radio astronomy @ low frequencies, you cannot ignore the ionosphere
- Mainly phase effect
- Variations in time, frequency and space
- You need to choose your calibration strategy well
 - Time, frequency solution interval
 - Transfer of calibrator solutions not sufficient → selfcal on target
- Rapid DD phase calibration necessary in many cases
- Polarised emission can be precorrected for ionospheric Faraday rotation using external data

Tutorial

- Download lofim.def, put it in an empty directory cd to that directory
- Start docker: `sudo service docker start`
- Check: `docker ps`
 - If you get permission denied : try `sudo chmod 666 /var/run/docker.sock`
- Build image: `docker build -t lofim_soft -f lofim.def ./` (this will take about an hour!)

Hopefully these first steps were already completed

- cd to directory with notebooks and materials (ionospheric_effects)
- Run image with docker: `run -it -v $PWD:/data -p 8000:8000 lofim_soft`
- `cd /data && jupyter lab --ip 0.0.0.0 --port 8000 --no-browser --allow-root`
- Open browser: open link from terminal
- Start notebook (Ionospheric Phase Effects.ipynb)