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Deep Learning in High Energy Physics

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What We Know: The Standard Model



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 $-\frac{1}{2}\partial_{\nu}g^a_{\mu}\partial_{\nu}g^a_{\mu} - g_s f^{abc}\partial_{\mu}g^a_{\nu}g^b_{\mu}g^c_{\nu} - \frac{1}{4}g^2_s f^{abc}f^{ade}g^b_{\mu}g^c_{\nu}g^d_{\mu}g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_{\mu}^a + \bar{G}^a\partial^2 G^a + g_s f^{abc}\partial_{\mu}\bar{G}^a G^b g_{\mu}^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- M^{2}W^{+}_{\mu}W^{-}_{\mu} - \frac{1}{2}\partial_{\nu}Z^{0}_{\mu}\partial_{\nu}Z^{0}_{\mu} - \frac{1}{2c^{2}}M^{2}Z^{0}_{\mu}Z^{0}_{\mu} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H$ $\frac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-} - M^{2}\phi^{+}\phi^{-} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2c^{2}}M\phi^{0}\phi^{0} - \beta_{h}[\frac{2M^{2}}{c^{2}} + \frac{1}{2}M\phi^{0}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2}\partial_{\mu}\phi^{0}$ $\frac{2M}{a}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)] + \frac{2M^4}{a^2}\alpha_h - igc_w[\partial_\nu Z^0_\mu(W^+_\mu W^-_\nu \begin{array}{l} W^+_{\nu} W^-_{\mu}) - Z^0_{\nu} (W^+_{\mu} \partial_{\nu} W^-_{\mu} - W^-_{\mu} \partial_{\nu} W^+_{\mu}) + Z^0_{\mu} (W^+_{\nu} \partial_{\nu} W^-_{\mu} - W^-_{\nu} \partial_{\nu} W^+_{\mu})] \\ - igs_w [\partial_{\nu} A_{\mu} (W^+_{\mu} W^-_{\nu} - W^+_{\nu} W^-_{\mu}) - A_{\nu} (W^+_{\mu} \partial_{\nu} W^-_{\mu} - W^-_{\nu} W^-_{\mu})] \\ \end{array}$ $W^{-}_{\mu}\partial_{\nu}W^{+}_{\mu}) + A_{\mu}(W^{+}_{\nu}\partial_{\nu}W^{-}_{\mu} - W^{-}_{\nu}\partial_{\nu}W^{+}_{\mu})] - \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\nu}W^{+}_{\nu}W^{-}_{\nu} +$ $\frac{1}{2}g^2W^+_{\mu}W^-_{\nu}W^+_{\mu}W^-_{\nu} + g^2c^2_w(Z^0_{\mu}W^+_{\mu}Z^0_{\nu}W^-_{\nu} - Z^0_{\mu}Z^0_{\mu}W^+_{\nu}W^-_{\nu}) + g^2s^2_w(A_{\mu}W^+_{\mu}A_{\nu}W^-_{\nu} - A_{\mu}A_{\mu}W^+_{\nu}W^-_{\nu}) + g^2s_wc_w[A_{\mu}Z^0_{\nu}(W^+_{\mu}W^-_{\nu} - A_{\mu}A_{\mu}W^+_{\nu}W^-_{\nu}) + g^2s^2_wc_w[A_{\mu}Z^0_{\nu}(W^+_{\mu}W^-_{\nu} - A_{\mu}A_{\mu}W^+_{\nu}W^-_{\nu})] + g^2s^2_wc_w[A_{\mu}Z^0_{\nu}(W^+_{\mu}W^-_{\mu} - A_{\mu}Z^0_{\nu}W^+_{\mu}W^-_{\nu})] + g^2s^2_wc_w[A_{\mu}Z^0_{\mu}Z^0_{\mu}W^+_{\mu}W^-_{\mu}] + g^2s^2_wc_w[A_{\mu}Z^0_{\mu}W^+_{\mu}W^-_{\mu}] + g^2s^2_wc_w[A_{\mu}Z^0_{\mu}W^+_{\mu}W^+_{\mu}W^-_{\mu}] + g^2s^2_wc_w[A_{\mu}Z^0_{\mu}W^+_{\mu}W^-_{\mu}] + g^2s^2_wc_w[A_{\mu}Z^0_{\mu}W^+_{\mu$ $W_{\nu}^{+}W_{\mu}^{-}) - 2A_{\mu}Z_{\mu}^{0}W_{\nu}^{+}W_{\nu}^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{+}\phi^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{-}\phi^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{0} + 2H\phi^{-}\phi^{-}] - g\alpha[H^{3} + H\phi^{0}\phi^{-}] - g\alpha[H^{3} +$ $\frac{1}{2}g^{2}\alpha_{h}[H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}]$ $gMW^+_{\mu}W^-_{\mu}H - \frac{1}{2}g\frac{M}{c^2}Z^0_{\mu}Z^0_{\mu}H - \frac{1}{2}ig[W^+_{\mu}(\phi^0\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^0) - \psi^0_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}$ $W^{-}_{\mu}(\phi^{0}\partial_{\mu}\phi^{+}-\phi^{+}\partial_{\mu}\phi^{0})]^{+}+\frac{1}{2}g[W^{+}_{\mu}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H)-W^{-}_{\mu}(H\partial_{\mu}\phi^{+}-\phi^{-}\partial_{\mu}H)]^{+}$ $(\phi^+ \partial_\mu H) + \frac{1}{2} g \frac{1}{c_{\mu}} (Z^0_{\mu} (H \partial_\mu \phi^0 - \phi^0 \partial_\mu H) - ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{\mu} (W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + ig \frac{s^2_w}{c_{\mu}} M Z^0_{$ $igs_w MA_\mu (W^+_\mu \phi^- - W^-_\mu \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z^0_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) +$ $igs_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^- \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^- \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^- \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^- \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^- \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^2 + (\phi^0)^2 + 2\phi^- \phi^-] - \frac{1}{4} g^2 W^+_\mu [H^$ $\frac{1}{4}g^{2}\frac{1}{c^{2}}Z_{\mu}^{0}Z_{\mu}^{0}[H^{2} + (\phi^{0})^{2} + 2(2s_{w}^{2} - 1)^{2}\phi^{+}\phi^{-}] - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} + \phi^{-})^{2}\phi^{+}\phi^{-}] - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} + \phi^{-})^{2}\phi^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} + \phi^{-})^{2}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} + \phi^{-})^{2}\phi^{0}(W_{\mu}^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} + \phi^{-})^{2}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{-}) - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}(W_{\mu}^{+}\phi^{ W_{\mu}^{-}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c}Z_{\mu}^{0}H(W_{\mu}^{+}\phi^{-} - W_{\mu}^{-}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W_{\mu}^{+}\phi^{-} +$ $W^-_{\mu}\phi^+) + \tfrac{1}{2}ig^2 s_w \tilde{A_{\mu}}H(W^+_{\mu}\phi^- - W^-_{\mu}\phi^+) - g^2 \tfrac{s_w}{c_w}(2c_w^2 - 1)Z^0_{\mu}\tilde{A_{\mu}}\phi^+\phi^- - g^2 \tfrac{s_w}{c_w}(2c_w^2 - 1)Z^0_{\mu}\tilde{A_{\mu}}\phi^- - g^2 \tfrac{s_w}C^0_{\mu}\tilde{A_{\mu}}\phi^- - g^2 \tfrac{s_w}{c_w$ $g^{1}s_{w}^{2}A_{\mu}\bar{A}_{\mu}\phi^{+}\phi^{-}-\bar{e}^{\lambda}(\gamma\partial+m_{e}^{\lambda})e^{\lambda}-\bar{\nu}^{\lambda}\gamma\partial\nu^{\lambda}-\bar{u}_{i}^{\lambda}(\gamma\partial+m_{e}^{\lambda})u_{i}^{\lambda} \bar{d}_i^{\lambda}(\gamma \partial + m_d^{\lambda})d_i^{\lambda} + igs_w A_{\mu}[-(\bar{e}^{\lambda}\gamma^{\mu}e^{\lambda}) + \frac{2}{3}(\bar{u}_i^{\lambda}\gamma^{\mu}u_i^{\lambda}) - \frac{1}{3}(\bar{d}_i^{\lambda}\gamma^{\mu}d_i^{\lambda})] +$ $\frac{ig}{4c} Z^{0}_{\mu} [(\bar{\nu}^{\lambda} \gamma^{\mu} (1+\gamma^{5}) \nu^{\lambda}) + (\bar{e}^{\lambda} \gamma^{\mu} (4s^{2}_{w} - 1 - \gamma^{5}) e^{\lambda}) + (\bar{u}^{\lambda}_{i} \gamma^{\mu} (\frac{4}{3}s^{2}_{w} - 1 - \gamma^{5}) e^{\lambda}) + (\bar{u}^{\lambda}_{i} \gamma^{\mu} (\frac{4}{3}s^{2}_{w} - 1 - \gamma^{5}) e^{\lambda}) + (\bar{u}^{\lambda}_{i} \gamma^{\mu} (1 - \gamma^{5}) e^{\lambda}) + (\bar{u}^{\lambda}_{i}$ $(1 - \gamma^5)u_j^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_w^2 - \gamma^5)d_j^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1 + \gamma^5)e^{\lambda}) + v_{\mu}^{\lambda}]$ $(\bar{u}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)C_{\lambda\kappa}d_j^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})] + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\prime}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^$ $\gamma^{5}(u_{j}^{\lambda})] + \frac{ig}{2\sqrt{2}} \frac{m_{e}^{\lambda}}{M} [-\phi^{+}(\bar{\nu}^{\lambda}(1-\gamma^{5})e^{\lambda}) + \phi^{-}(\bar{e}^{\lambda}(1+\gamma^{5})\nu^{\lambda})] \frac{g}{2}\frac{m_e^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\phi^0(\bar{e}^{\lambda}\gamma^5 e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\phi^+[-m_d^{\kappa}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}) + \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})] + \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa}) - \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M_{\lambda}/2}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M_{\lambda}/2}\phi$ $\gamma^5 u_i^{\kappa}] - \frac{g}{2} \frac{m_u^{\lambda}}{M} H(\bar{u}_i^{\lambda} u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} H(\bar{d}_i^{\lambda} d_i^{\lambda}) + \frac{ig}{2} \frac{m_u^{\lambda}}{M} \phi^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) \frac{ig}{2} \frac{m_d^{\lambda}}{M} \phi^0(\bar{d}_i^{\lambda} \gamma^5 d_i^{\lambda}) + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - M^2) X^ \frac{M^2}{c^2}$) $X^0 + \bar{Y}\partial^2 Y + igc_w W^+_\mu (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + igs_w W^+_\mu (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ X^0)$ $\partial_{\mu}\bar{X}^{+}Y) + igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{X}^{0}X^{+}))$ $\partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{$ $\partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c^{2}}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_w^2}{2c_w}igM[\bar{X}^+X^0\phi^+ - \bar{X}^-X^0\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-]$ $\bar{i} g M s_w [\bar{X}^0 X^- \phi^+ - \bar{X}^0 X^+ \phi^-] + \frac{1}{2} \bar{i} g M [\bar{X}^+ X^+ \phi^0 - \bar{X}^- X^- \phi^0]$

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What We Know: The Standard Model

Symbol	Description	Value
m _e	Electron mass	511 keV
m _µ	Muon mass	105.7 MeV
mτ	Tau mass	1.78 GeV
mu	Up quark mass	1.9 MeV
m _d	Down quark mass	4.4 MeV
ms	Strange quark mass	87 MeV
mc	Charm quark mass	1.32 GeV
m _b	Bottom quark mass	4.24 GeV
<i>m</i> t	Top quark mass	172.7 GeV
θ_{12}	CKM 12-mixing angle	13.1°
$ heta_{23}$	CKM 23-mixing angle	2.4°
<i>0</i> 13	CKM 13-mixing angle	0.2°
δ	CKM CP-violating Phase	0.995
g_1	U(1) gauge coupling	0.357
g_2	SU(2) gauge coupling	0.652
g ₃	SU(3) gauge coupling	1.221
θ_{QCD}	QCD vacuum angle	~0
V	Higgs vacuum expectation value	246 GeV
m _н	Higgs mass	125 GeV

 $-\tfrac{1}{2}\partial_{\nu}g^a_{\mu}\partial_{\nu}g^a_{\mu} - g_s f^{abc}\partial_{\mu}g^a_{\nu}g^b_{\mu}g^c_{\nu} - \tfrac{1}{4}g^2_s f^{abc}f^{ade}g^b_{\mu}g^c_{\nu}g^d_{\mu}g^e_{\nu} +$ $\frac{1}{2}ig_s^2(\bar{q}_i^{\sigma}\gamma^{\mu}q_i^{\sigma})g_{\mu}^a + \bar{G}^a\partial^2 G^a + g_s f^{abc}\partial_{\mu}\bar{G}^a G^b g_{\mu}^c - \partial_{\nu}W_{\mu}^+\partial_{\nu}W_{\mu}^- M^{2}W^{+}_{\mu}W^{-}_{\mu} - \frac{1}{2}\partial_{\nu}Z^{0}_{\mu}\partial_{\nu}Z^{0}_{\mu} - \frac{1}{2c^{2}}M^{2}Z^{0}_{\mu}Z^{0}_{\mu} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H - \frac{1}{2}\partial_{\mu}H\partial_{\mu}H$ $\frac{1}{2}m_{h}^{2}H^{2} - \partial_{\mu}\phi^{+}\partial_{\mu}\phi^{-} - M^{2}\phi^{+}\phi^{-} - \frac{1}{2}\partial_{\mu}\phi^{0}\partial_{\mu}\phi^{0} - \frac{1}{2c^{2}}M\phi^{0}\phi^{0} - \beta_{h}[\frac{2M^{2}}{c^{2}} +$ $\frac{2M}{a}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)] + \frac{2M^4}{a^2}\alpha_h - igc_w[\partial_\nu Z^0_\mu(W^+_\mu W^-_\nu \begin{array}{l} W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\ddot{\partial}_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})] \\ - igs_{w}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\mu}^{-})] \\ - igs_{\nu}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\mu}^{-})] \\ - igs_{\nu}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\nu}^{-})] \\ - igs_{\nu}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{-}W_{\mu}^{-}] \\ - igs_{\nu}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{-}W_{\mu}^{-}]] \\ - igs_{\nu}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{-}W_{\mu}^{-}] \\ - igs_{\nu}[\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{-}W_{\mu}^{-}]] \\ - igs_{\nu}[\partial_{\nu}A_{\nu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{-}W_{\nu}^{-}]] \\ - igs_{\nu}[\partial_{\nu}A_{\nu}(W_{\nu}^{+}W_{\nu}^{-}W_{\nu}^{-}W_{\nu}^{-}]] \\ - igs_{\nu}[\partial_{\nu}A_{\nu}(W_{\nu}^{+}W_{\nu}^{-}W_{$ $W^{-}_{\mu}\partial_{\nu}W^{+}_{\mu}) + A_{\mu}(W^{+}_{\nu}\partial_{\nu}W^{-}_{\mu} - W^{-}_{\nu}\partial_{\nu}W^{+}_{\mu})] - \frac{1}{2}g^{2}W^{+}_{\mu}W^{-}_{\mu}W^{+}_{\nu}W^{-}_{\nu} +$ $\frac{1}{2}g^2W^+_{\mu}W^-_{\nu}W^+_{\mu}W^-_{\nu} + g^2c^2_w(Z^0_{\mu}W^+_{\mu}Z^0_{\nu}W^-_{\nu} - Z^0_{\mu}Z^0_{\mu}W^+_{\nu}W^-_{\nu}) +$ $g^{2}s_{w}^{2}(A_{\mu}W_{\mu}^{+}A_{\nu}W_{\nu}^{-}-A_{\mu}A_{\mu}W_{\nu}^{+}W_{\nu}^{-})+g^{2}s_{w}c_{w}[A_{\mu}Z_{\nu}^{0}(W_{\mu}^{+}W_{\nu}^{-} W^+_{\nu}W^-_{\mu}) - 2A_{\mu}Z^0_{\mu}W^+_{\nu}W^-_{\nu}] - g\alpha[H^3 + H\phi^0\phi^0 + 2H\phi^+\phi^-] \frac{1}{2}g^{2}\alpha_{h}[H^{4} + (\phi^{0})^{4} + 4(\phi^{+}\phi^{-})^{2} + 4(\phi^{0})^{2}\phi^{+}\phi^{-} + 4H^{2}\phi^{+}\phi^{-} + 2(\phi^{0})^{2}H^{2}]$ $gMW^+_{\mu}W^-_{\mu}H - \frac{1}{2}g\frac{M}{c^2}Z^0_{\mu}Z^0_{\mu}H - \frac{1}{2}ig[W^+_{\mu}(\phi^0\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^0) - \psi^0_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}\phi^- - \psi^0_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}\partial_{\mu}$ $W_{\mu}^{-}(\phi^{0}\partial_{\mu}\phi^{+}-\phi^{+}\partial_{\mu}\phi^{0})] + \frac{1}{2}g[W_{\mu}^{+}(H\partial_{\mu}\phi^{-}-\phi^{-}\partial_{\mu}H) - W_{\mu}^{-}(H\partial_{\mu}\phi^{+}-\phi^{-}\partial_{\mu}H) - W_{\mu}^{-}(H\partial_{\mu}\phi^{+}-\phi^{-}) - W_{\mu}^{-}(H\partial_{\mu}\phi^{+}-\phi^{$ $\phi^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{c_{\mu}}(Z^{0}_{\mu}(H\partial_{\mu}\phi^{0} - \phi^{0}\partial_{\mu}H) - ig\frac{s^{2}_{w}}{c_{\mu}}MZ^{0}_{\mu}(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) +$ $igs_w MA_\mu (W^+_\mu \phi^- - W^-_\mu \phi^+) - ig \frac{1-2c_w^2}{2c_w} Z^0_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) +$ $igs_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - \frac{1}{4} g^2 W^+_\mu W^-_\mu [H^2 + (\phi^0)^2 + 2\phi^+ \phi^-] \frac{1}{4}g^{2}\frac{1}{c^{2}}Z_{\mu}^{0}Z_{\mu}^{0}[H^{2} + (\phi^{0})^{2} + 2(2s_{w}^{2} - 1)^{2}\phi^{+}\phi^{-}] - \frac{1}{2}g^{2}\frac{s_{w}^{2}}{c_{w}}Z_{\mu}^{0}\phi^{0}(W_{\mu}^{+}\phi^{-} +$ $W^{-}_{\mu}\phi^{+}) - \frac{1}{2}ig^{2}\frac{s_{w}^{2}}{c_{w}}Z^{0}_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) + \frac{1}{2}g^{2}s_{w}A_{\mu}\phi^{0}(W^{+}_{\mu}\phi^{-} +$ $W^{-}_{\mu}\phi^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W^{+}_{\mu}\phi^{-} - W^{-}_{\mu}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z^{0}_{\mu}A_{\mu}\phi^{+}\phi^{-} - W^{-}_{\mu}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z^{0}_{\mu}A_{\mu}\phi^{+}\phi^{-}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2} - 1)Z^{0}_{\mu}A_{\mu}\phi^{-}) - g^{2}\frac{s_{w}$ $g^1 s_w^2 A_\mu A_\mu \phi^+ \phi^- - \bar{e}^\lambda (\gamma \partial + m_e^\lambda) e^\lambda - \bar{\nu}^\lambda \gamma \partial \bar{\nu}^\lambda - \bar{u}_i^\lambda (\gamma \partial + m_\mu^\lambda) u_i^\lambda \bar{d}_i^{\lambda}(\gamma \partial + m_d^{\lambda})d_i^{\lambda} + igs_w A_{\mu}[-(\bar{e}^{\lambda}\gamma^{\mu}e^{\lambda}) + \frac{2}{3}(\bar{u}_i^{\lambda}\gamma^{\mu}u_i^{\lambda}) - \frac{1}{3}(\bar{d}_i^{\lambda}\gamma^{\mu}d_i^{\lambda})] +$ $\frac{ig}{4c}Z^0_\mu[(\bar{\nu}^\lambda\gamma^\mu(1+\gamma^5)\nu^\lambda)+(\bar{e}^\lambda\gamma^\mu(4s^2_w-1-\gamma^5)e^\lambda)+(\bar{u}^\lambda_i\gamma^\mu(\frac{4}{2}s^2_w (1 - \gamma^5)u_j^{\lambda}) + (\bar{d}_j^{\lambda}\gamma^{\mu}(1 - \frac{8}{3}s_w^2 - \gamma^5)d_j^{\lambda})] + \frac{ig}{2\sqrt{2}}W_{\mu}^+[(\bar{\nu}^{\lambda}\gamma^{\mu}(1 + \gamma^5)e^{\lambda}) + v_{\mu}^{\lambda}]$ $(\bar{u}_j^{\lambda}\gamma^{\mu}(1+\gamma^5)C_{\lambda\kappa}d_j^{\kappa})] + \frac{ig}{2\sqrt{2}}W_{\mu}^{-}[(\bar{e}^{\lambda}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda})] + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\dagger}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^{\prime}\gamma^{\mu}(1+\gamma^5)\nu^{\lambda}) + (\bar{d}_j^{\kappa}C_{\lambda\kappa}^$ $\gamma^5 u_j^{\lambda}$] + $\frac{ig}{2\sqrt{2}} \frac{m_e^{\lambda}}{M} [-\phi^+(\bar{\nu}^{\lambda}(1-\gamma^5)e^{\lambda}) + \phi^-(\bar{e}^{\lambda}(1+\gamma^5)\nu^{\lambda})] \frac{g}{2}\frac{m_e^{\lambda}}{M}[H(\bar{e}^{\lambda}e^{\lambda}) + i\phi^0(\bar{e}^{\lambda}\gamma^5 e^{\lambda})] + \frac{ig}{2M\sqrt{2}}\phi^+[-m_d^{\kappa}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1-\gamma^5)d_j^{\kappa}) +$ $m_u^{\lambda}(\bar{u}_j^{\lambda}C_{\lambda\kappa}(1+\gamma^5)d_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa}) - m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa}) - \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa}] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}}\phi^{-}[m_d^{\lambda}(1+\gamma^5)u_j^{\kappa})] + \frac{ig}{2M\sqrt{2}$ $\gamma^5 u_i^{\kappa}] - \frac{g}{2} \frac{m_u^{\lambda}}{M} H(\bar{u}_i^{\lambda} u_i^{\lambda}) - \frac{g}{2} \frac{m_d^{\lambda}}{M} H(\bar{d}_i^{\lambda} d_i^{\lambda}) + \frac{ig}{2} \frac{m_u^{\lambda}}{M} \phi^0(\bar{u}_i^{\lambda} \gamma^5 u_i^{\lambda}) \frac{ig}{2} \frac{m_d^{\lambda}}{M} \phi^0(\bar{d}_i^{\lambda} \gamma^5 d_i^{\lambda}) + \bar{X}^+ (\partial^2 - M^2) X^+ + \bar{X}^- (\partial^2 - M^2) X^- + \bar{X}^0 (\partial^2 - M^2) X^ \frac{M^2}{c^2}$) $X^0 + \bar{Y}\partial^2 Y + igc_w W^+_\mu (\partial_\mu \bar{X}^0 X^- - \partial_\mu \bar{X}^+ X^0) + igs_w W^+_\mu (\partial_\mu \bar{Y} X^- - \partial_\mu \bar{X}^+ X^0)$ $\partial_{\mu}\bar{X}^{+}Y) + igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{X}^{0}X^{+}))$ $\partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{X}^{-}X^{-}) + igs_{w}A_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+})$ $\partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM[\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{2}\bar{X}^{0}X^{0}H] +$ $\frac{1-2c_w^2}{2c_w}igM[\bar{X}^+X^0\phi^+ - \bar{X}^-X^0\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-] + \frac{1}{2c_w}igM[\bar{X}^0X^-\phi^-]$ $igMs_w[\bar{X}^0X^-\phi^+ - \bar{X}^0X^+\phi^-] + \frac{1}{2}igM[\bar{X}^+X^+\phi^0 - \bar{X}^-X^-\phi^0]$

The Standard Model in Action



What are we missing?

- Is the Higgs boson connected to New Physics?
- Why Gravity so much weaker then the other forces?
- What are Dark Matter and Dark Energy?
- What gives neutrinos their mass?
- Why is there a matter /anti-matter asymmetry?

- New forces and heavy particles may have been active during the early universe that explain these phenomena
- We can look for them in high energy physics experiments!
- How can machine learning help?



The ATLAS Experiment

 $\sim 10^8$ detector channels

<u>Data:</u> ~300 MB / sec ~3000 TB / year

<u>Weight:</u> 7000 tons <u>Size:</u> 46 m long, 25 m high, 25 m wide







• Causal and Compositional Structure

Collision \rightarrow particle X \rightarrow "final state" particles \rightarrow detector data



• Causal and Compositional Structure

particle X ← "final state" particles ← detector data



• Reconstruction: Find the "final state" particles in the detector



• Add them together to study underlying collision





• Works because of energy and momentum conservation:

$$(E_{\mathbf{X}}, \vec{p}_{\mathbf{X}}) = \sum (E_i, \vec{p}_i)$$

 $i \in \text{decay products}$

$$M_{
m X}c^2=\sqrt{E_{
m X}^2}$$
 - $ec{p_{
m X}}^2$ c^2



• Multiple processes contribute to same signature









- With a collection of collisions we can perform:
 - Hypothesis testing: new particle present?
 - Measurement: Inference of latent parameters, e.g. Higgs mass
- Extremely accurate simulations + knowledge of the data generating process (i.e. physics) to analyze our data!

From Theory to Experiment

O(10) particles

$$\begin{split} &-\frac{1}{4}\partial_{y}Q_{0}\partial_{y}Q_{0}^{-}-g_{1}A^{0}\partial_{y}Q_{0}^{+}Q_{0$$

 $\begin{array}{l} \gamma^5(y_2^*)] = \frac{1}{2\eta_2^*} \frac{2\eta_1^*}{2\eta_1^*} \Big(-\phi^+(\dot{\nu}^A(1-\gamma^5)\nu^+) + \phi^-(\dot{\nu}^A(1+\gamma^5)\nu^A) \Big) - \\ \frac{2}{3} \frac{\eta_2^*}{3\eta_1^*} \Big(H(\dot{\nu}^A \nu^+) + i\phi^B(\dot{\nu}^+ \gamma^A \nu^+) + \frac{\eta_2^*}{2\eta_1^*} \phi^+(-m_q^*(\dot{\eta}^A C_{-k}(1-\gamma^2)d_1^*) + \\ -m_q^*(\dot{\mu}^A C_{-k}(1-\gamma^2)d_1^*) + \frac{\eta_2^*}{2\eta_1^*} \frac{\eta_2^*}{2\eta_1^*} \phi^+(\eta_1^*d_1^*d_1^*) + \frac{\eta_1^*}{2\eta_1^*} \phi^*(\dot{\mu}^A \gamma^A \nu^+) \\ - \gamma^5(y_1^*) = \frac{2}{3} \frac{\eta_1^*}{4\eta_1^*} H(\dot{\mu}^A \eta_1^*) = \frac{2}{3} \frac{\eta_1^*}{4\eta_1^*} H(\dot{d}^A \eta_1^*) + \frac{2}{3} \frac{\eta_2^*}{3\eta_1^*} \phi^*(\dot{\mu}^A \gamma^A \eta_1) - \\ \end{array}$

 $\begin{array}{l} 1 & \|u\|_{1}^{-1} \leq \frac{\pi}{2}M(\partial_{1}u_{1}) \leq \frac{\pi}{2}M(\partial_{1}u_{1}) + \frac{\pi}{2}M'(u_{1}^{-1}u_{1}) + \frac{\pi}{2}M'(u_{1}^{-1}u_{1}) + \frac{\pi}{2}M'(u_{1}^{-1}u_{1}) + \frac{\pi}{2}M'(u_{1}^{-1}u_{1}) - \frac{\pi}{2}M'(u_{1}^{-1}u_{1}) + \frac{$

 $\begin{array}{l} \frac{1-2a_{w}^{2}}{2c_{w}}igM[\bar{X}^{+}X^{0}\phi^{+}-\bar{X}^{-}X^{0}\phi^{-}]+\frac{1}{2c_{w}}igM[\bar{X}^{0}X^{-}\phi^{+}-\bar{X}^{0}X^{+}\phi^{-}]+\\ igMs_{w}[\bar{X}^{0}X^{-}\phi^{+}-\bar{X}^{0}X^{+}\phi^{-}]+\frac{1}{2}igM[\bar{X}^{+}X^{+}\phi^{0}-\bar{X}^{-}X^{-}\phi^{0}] \end{array}$



O(100) particles

O(10⁸) detector elements

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From Theory to Experiment

g

.....

W

Η

 $\begin{array}{c} -\frac{1}{2}\partial_{s}q_{0}^{0}\partial_{s}g_{0}^{s}-g_{0}J^{bb}\partial_{s}q_{0}^{s}g_{0}^{s}g_{0}^{s}-\frac{1}{2}g_{0}^{2}J^{bb}f^{ab}g_{0}^{bb}g_{0}^{s}g_{0}^{s}g_{0}^{s}+,\\ +\frac{1}{2}(g_{0}^{s}(q_{0}^{s})q_{0}^{s})g_{0}^{s}+C^{b}C^{b}C^{s}+g_{0}J^{b}\partial_{s}C^{b}C^{s}g_{0}^{s}-\partial_{s}W^{b}\partial_{s}W^{s}-\\ M^{2}W^{b}_{w}W_{w}^{-\frac{1}{2}}\partial_{w}Z^{b}\partial_{s}Z^{b}-\frac{1}{2}g_{0}Z^{b}Z^{b}Z^{b}Z^{b}Z^{b}Z^{b}-\frac{1}{2}\partial_{s}A\partial_{0}A_{w}-\frac{1}{2}\partial_{w}H^{2}\partial_{b}W^{s}-\\ +\frac{1}{2}g_{0}H^{2}-\partial_{0}C^{b}\partial_{v}C^{s}-\frac{1}{2}\partial_{s}Q^{b}\partial_{s}Q^{b}-\frac{1}{2}g_{0}M^{b}Q^{b}D^{b}-\beta_{0}[\frac{12d}{y}^{b}+\\ \frac{2M}{y}H+\frac{1}{2}(H^{2}+\phi^{0}\phi^{b}+2\phi^{+}\phi^{-})]+\frac{2M}{y}h_{w}\alpha_{w}-(g_{0}\partial_{s}Z^{b}(W^{w})W_{w}^{s}-\\ \end{array}$

$$\begin{split} & \frac{a_{10}}{2} H + \frac{1}{2} (H^+ \phi^+ \phi^+ Z^0 \phi^-) + \frac{a_{10}}{2} - a_{0--} \log c_{10} \partial_{z_{1}} Z^0_{10} (W^+_{2} W^-_{2} - W^+_{2} W^+_{2}) + 2 Z^0_{10} (W^+_{2} W^-_{2} - W^+_{2} W^+_{2}) - 2 Z^0_{10} (W^+_{2} W^-_{2} - W^-_{2} W^+_{2}) - 2 Z^0_{10} (W^+_{2} W^-_{2} - W^-_{2} W^+_{2}) - 2 Z^0_{10} W^-_{10} W^+_{10} W^-_{10} - 2 Z^0_{10} (W^+_{2} W^-_{2} - W^-_{2} W^+_{10}) - 2 Z^0_{10} W^-_{10} W^+_{10} W^-_{10} - 2 Z^0_{10} W^-_{10} W^+_{10} W^-_{10} - 2 Z^0_{10} W^-_{10} W^+_{10} W^-_{10} + 2 Z^0_{10} Z^0_{10} W^-_{10} W^+_{10} W^-_{10} - 2 Z^0_{10} W^-_{10} W^+_{10} + 2 Z^0_{10} W^-_{10} W^-_{$$
 $y = (\psi_{0}(+\mu)^{-}) + (\psi_{0}$

 $\begin{array}{l} \frac{g}{g}\sigma_{0h}[n^{-+}(\psi^{-})^{-+}4(\psi^{-})\phi^{-}] + \frac{4}{2}(\psi^{-})\phi^{-}\phi^{-}) + \frac{4}{2}(\psi^{-})\phi^{-}\phi^{-}) + \frac{1}{2}(\psi^{-})\phi^{-}\phi^{-}) \\ gMW_{\mu}^{+}W_{\mu}^{+}M - \frac{1}{2}\frac{g}{g}\frac{g}{c}^{+}\omega^{-}g^{-}M + \frac{1}{2}g(W_{\mu}^{+}(H\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}H) - W_{\mu}^{-}(H\partial_{\mu}\phi^{+} - \phi^{+}\partial_{\mu}H)] + \frac{1}{2}g\frac{1}{2}(\omega^{-})g^{-}Q^{-}\partial_{\mu}H + \frac{1}{2}g(W_{\mu}^{+}(H\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}H) - \frac{1}{2}g\frac{g}{c}^{+}MZ_{\mu}^{0}(W_{\mu}^{+}\phi^{-} - W_{\mu}^{-}\phi^{+}) + \end{array}$

 $\begin{array}{c} igs_w MA_{\mu}(W_{\mu}^+\phi^- - W_{\mu}^-\phi^+) - ig\frac{1-2c_w^2}{2c_w}Z_{\mu}^0(\phi^+\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^+) + \\ igs_w A_{\mu}(\phi^+\partial_{\mu}\phi^- - \phi^-\partial_{\mu}\phi^+) - \frac{1}{4}g^2W_{\mu}^+W_{\mu}^-[H^2 + (\phi^0)^2 + 2\phi^+\phi^-] - \end{array}$



From Theory to Experiment





- Build on our knowledge of how the data is created
 - Use our simulation to design and study reconstruction algorithms, and to compare predictions with our experimental data
- Use Machine learning to improve (or rethink) the steps of this process?

Machine Learning Applied Widely in HEP

• In analysis:

- Classifying signal from background, especially in complex final states
- Reconstructing heavy particles and improving the energy / mass resolution

• In reconstruction:

- Improving detector level inputs to reconstruction
- Particle identification tasks
- Energy / direction calibration

• In the trigger:

- Quickly identifying complex final states

• In computing:

 Estimating dataset popularity, and determining needed number and location of dataset replicas



Deep Learning for HEP

- How do we move deep learning advancements into HEP?
 - Translate problems in HEP into problems in ML domain
 - Incorporate HEP domain knowledge when building models
 - How do we extract what is learned?





Jets at the LHC





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Machine Learning and Jet Physics



- Can use internal structure of a jet for classification
 Also known as Jet Substructure
- A wealth of domain expertise has gone in feature engineering
- Can deep learning perform this classification?

Jet Images

Unrolled slice of detector



Calorimeter towers as pixels Energy depositions as intensity

Jet Images

10⁻⁸ 10⁻⁹

jet image $250 < p_T/GeV < 260 GeV, 65 < mass/GeV < 95$ Pythia 8, W' \rightarrow WZ, $\sqrt{s} = 13 \text{ TeV}$ Pixel p_T [GeV] 10² 10 0.5 10-1 10⁻² et W-jets 10⁻³ 10-4 10⁻⁵ -0.5 10⁻⁶ proton-proton ϕ 10-7 collision into/ 10⁻⁸ out-of page 10⁻⁹ -1 -0.5 0 0.5 [Translated] Pseudorapidity (n) jet 250 < p_{_}/GeV < 260 GeV, 65 < mass/GeV < 95 Pythia 8, QCD dijets, $\sqrt{s} = 13 \text{ TeV}$ 0^{3} Pixel p_r [GeV] [Translated] Azimuthal Angle (<a) 10² 10 not to scale 0.5 10-1 QCD-jets 10⁻² jet image 10⁻³ 10-4 10⁻⁵ -0.5 10⁻⁶ 10⁻⁷

B. Nachman: https://indico.cern.ch/event/567550/contributions/2656471/

Average of large number of Jet Images

-1

-0.5

0

0.5

[Translated] Pseudorapidity (n)

Deep Jets – Convolutional Neural Networks



Performance with Deep Neural Networks



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Learning from the Machines

arXiv:1511:05190







Beyond Images: New representations, models, and applications for deep learning in jet physics



I. Henrion et. al., presented at NIPS workshop on deep learning for physics sciences

0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9

Signal efficiency



Generative Adversarial Networks (GAN)





- Full Simulation: accurate simulation of particle interactions with material
 - Computationally very costly
 - Only produce sample, can't compute analytically P(energy deposits | particle)
- Fast Simulation: simplified parametric model of energy deposits
- Generative models to learn data distribution, p(x), and produce samples?
 - Generative Adversarial Networks (GAN)
 - Variational Auto-Encoders (VAE)

GANs

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- Generator produces images from random noise and tries to trick discriminator into thinking they are real
- Classifier tries to tell the difference between real and fake images

Images: arXiv:1710.10196

GANs for HEP



• GANs and VAEs being studied for generating Jet-images, and 3D calorimeter energy depositions in toy simulation and at the LHC experiments!





- Developing new ways to train our algorithms. Examples:
 - Parametrized learning [EPJ C76 (2016) no.5, 235]
 - Adversarial learning to pivot [NIPS 2017, 1611.01046]
 - Learning from label proportions [1702.00414]

Dealing with Systematic Uncertainties

- Systematic uncertainties encapsulate our incomplete knowledge of physical processes and detectors
- Can we teach a classifier to be robust to these kinds of uncertainties?



Adversarial Networks



• Classifier built to solve problem at hand

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Adversarial Networks





- Systematic uncertainty encoded as nuisance parameters, Z
- Adversary to predict the value of Z given classifier output

$$\hat{\theta}_f, \hat{\theta}_r = \arg\min_{\theta_f} \max_{\theta_r} E(\theta_f, \theta_r).$$

$$E_{\lambda}(\theta_f, \theta_r) = \mathcal{L}_f(\theta_f) - \lambda \mathcal{L}_r(\theta_f, \theta_r),$$



- Loss encodes performance of classifier and adversary

 Classifier penalized when adversary does well at predicting Z
- Hyper-parameter λ controls trade-off
 - Large λ enforces f(...) to be pivotal, e.g. robust to nuisance
 - Small λ allows f(...) to be more optimal

Learning to Pivot: Physics Example

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- λ=0, Z=0
 - Standard training with no systematics during training, evaluate systematics after training
- λ=0
 - Training samples include events with systematic variations, but no adversary used

• λ=10

 Trading accuracy for robustness results in net gain in terms of statistical significance

- Better understanding how to use computer vision and natural language processing techniques
- Thinking about new data structures, like trees and graphs, that can be analyzed with Deep Learning



I. Henrion et. al., presented at NIPS workshop on deep learning for physics sciences

arXiv:1707.08600

arXiv:1702.00748

- Better understanding how to use computer vision and natural language processing techniques
- Thinking about new data structures, like trees and graphs, that can be analyzed with Deep Learning
- Can ML help with our most computationally costly problems, like simulation or the combinatorial challenge of tracking?





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- Better understanding how to use computer vision and natural language processing techniques
- Thinking about new data structures, like trees and graphs, that can be analyzed with Deep Learning
- Can ML help with our most computationally costly problems, like simulation or the combinatorial challenge of tracking?
- Can fast O(ns-µs) NN inference be done with FPGAs to put ML early in the trigger / data acquisition process?
- Can we design better architectures and training algorithms to tackle our HEP challenges?
- How can we make best use of our simulation for inference without the PDF, i.e. Likelihood Free Inference?

Conclusion

• Just touched the surface of the rapid progress in Machine Learning in HEP

• Deep learning application developing quickly in High Energy Physics, across the whole data acquisition, simulations, and analysis pipeline

 Many new developments and performance improvements driven by thinking about HEP challenges in completely new ways



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Generative Model

- Build on our knowledge of how the data is created
 - Use our simulation to design and study reconstruction algorithms, and to compare predictions with our experimental data
- Use Machine learning to improve (or rethink) the steps of this process?

Simulation



p(*particles* | *interation type*)



p(*detector signature* | *particle*)





Particle identification = Classification

 $p(\text{electron} \mid \text{data})$

Energy estimation = Inference, regression

 $p(E_{\text{true}}^{\text{electron}} \mid \text{electron data})$

Understanding Clusters of Particles: Jets



- **Jet**: stream of particles produced by high energy quarks and gluons
 - Clustering algorithms used to find them
- Jet identification = Classification

p(*parent particle* | *jet cluster*)

• Energy estimation = Inference, regression

 $p(E_{true}^{jet} \mid jet \ cluster)$

Analyzing Events and Hypothesis Testing

Analyzing Events





Hypothesis Testing and Parameter Estimation





Phys. Lett. B 726 (2013)

Decorrelating Variables

- arXiv:1703.03507
- Same adversarial setup can decorrelate a classifier from a chosen variable (rather than nuisance parameter)
- In this example, decorrelate classifier from jet mass, so as not to sculpt jet mass distribution with classifier cut





Generative Model

Neutrino Identification at NOvA





- Two 2D projections of the interactions
- Goal: discriminate between different neutrino interactions / backgrounds



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Neutrino Identification at NOvA

arXiv:1604.01444



- Two 2D projections of the interactions
- Goal: discriminate between different neutrino interactions / backgrounds
- Make use of powerful computer vision architectures, here GoogLeNet, and adapt to our challenges



Neutrino Identification at NOvA

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- Convolution filters and outputs show interesting features about how the NN is providing discrimination
- Major gains over current algorithms in v_e -CC discrimination: 35% \rightarrow 49% signal efficiency for the same background rejection